

What can we apply MSA / classifications to?

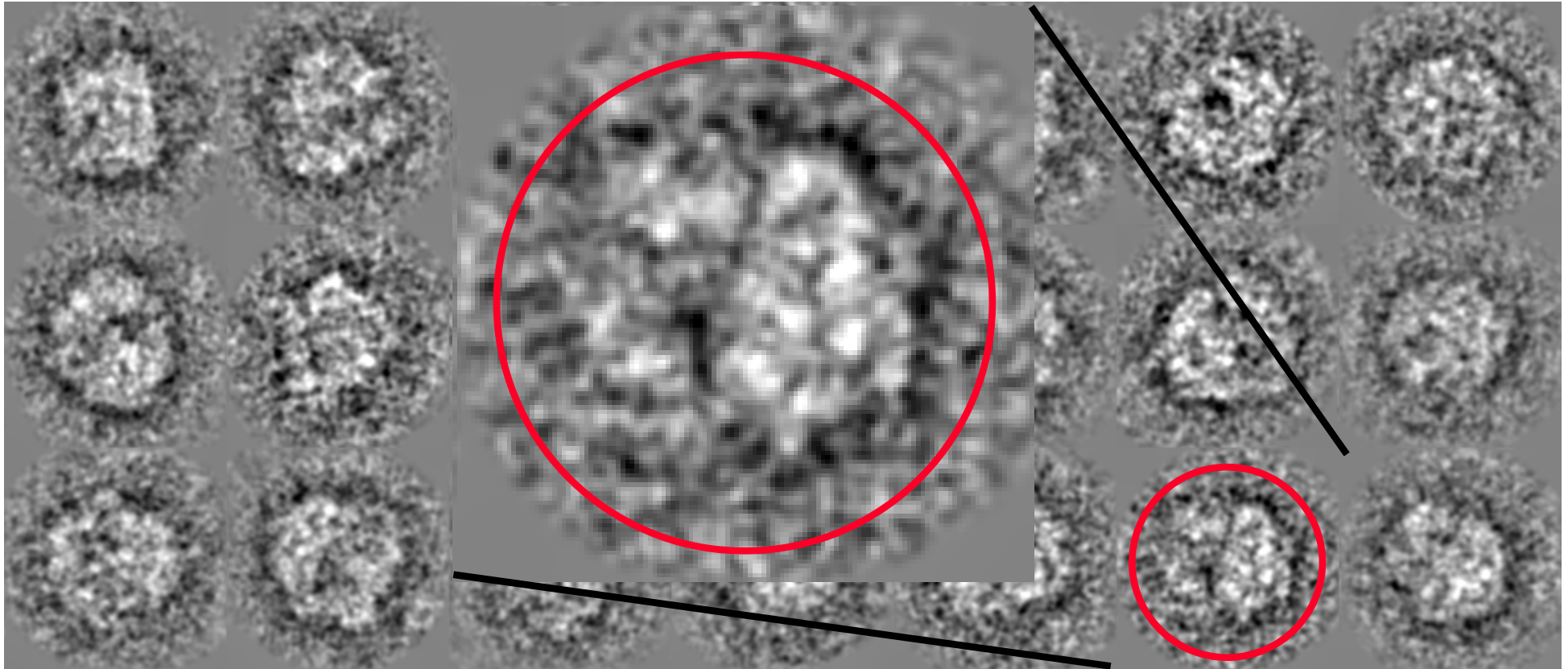
- 2D classification (reference-free alignment: only centered data, not rotationally aligned)
- alignment by classification (alignment against class averages or a typical eigenimage)
- analysis of symmetry (through symmetry in the eigenimages)
- local MSA (focus on an area with high structural variability)
- re-classification of class averages belonging to an object view
- size-classification (e.g. White et al., *J. Mol. Biol.* 336 (2004) 453-460).
- 3D classification of structures (separation of mixed particle populations):
particles:3D-SC, sub-tomograms
- classification of powerspectra (sorting of defocus classes)

Important to do before MSA:

- normalisation
- filtering
- centered data (aligned if for structure refinement)
- define MSA area: MSA mask



Example of initial class averages:



70S ribosome data set, 500 particles, 50 classes, ~10 members per class
band-pass filter: 300Å - 12Å; *Imagic*

Now find your Euler angles and start the structure...!

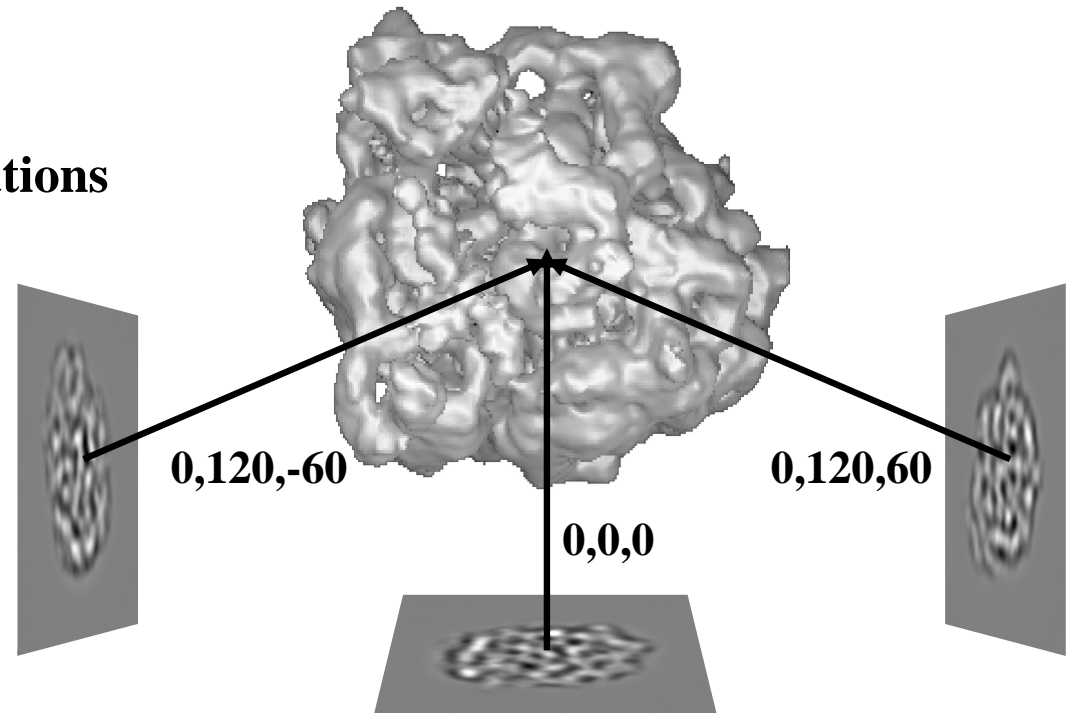
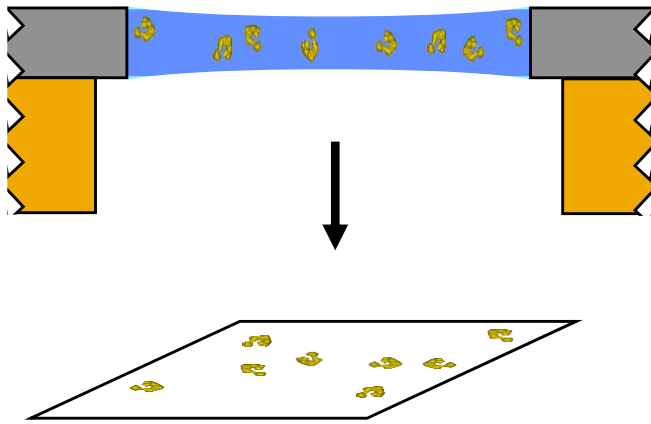
But will it work?

Structure determination by 3D reconstruction

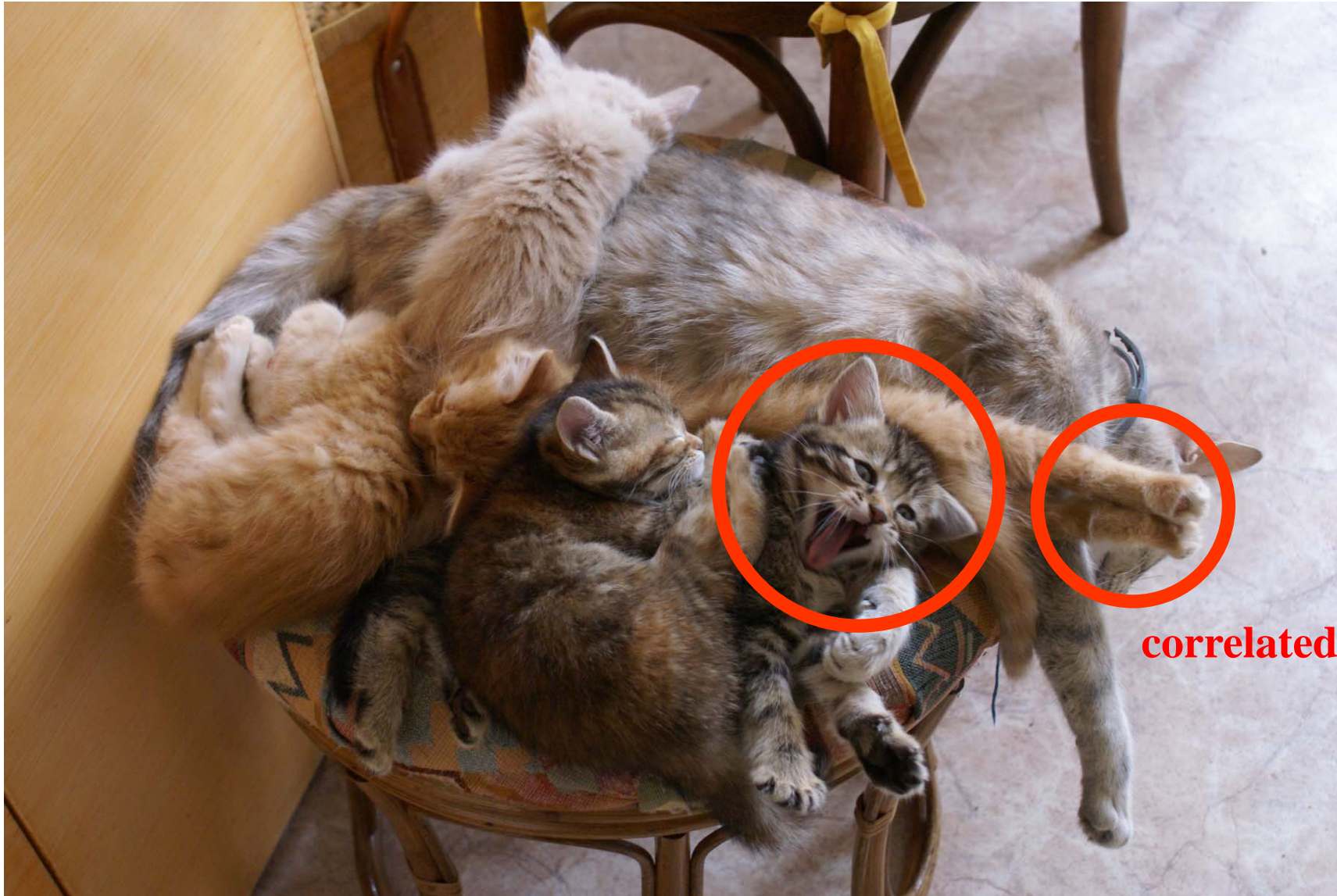
Assumptions?

3D reconstruction of single particles:

unique particle type in **random** orientations



And what if we have different structures in the sample...?
Conformational changes of cats?



Different conformations? → Cannot be averaged

What means homogeneity?

- same composition**
- same functional state**
- same structural state, i.e. same conformational state**

Determining structures of multiple conformational states in a single sample

Homogeneity of multi-component system / macromolecular complexes is tricky to get:

- multiple subunits / components (proteins, RNA, DNA,...)
- flexibility of the core structure

Additional, dynamic components:

- factors such as proteins, RNA, DNA binding transiently
- nucleotides (GTP +/- hydrolysable)
- ligands

Determining structures of multiple conformational states in a single sample

Sample heterogeneity:

- typical problem of multi-component systems, composition & flexibility
- structure determination difficult / limits resolution
- detection of the problem: disordered 3D map; MSA
- **advantage:** analysis of dynamics

Structure sorting has important implications for high-resolution structural studies and allows converting the problem of heterogeneity into an advantage by describing structure ensembles to provide insights into the dynamics of multi-component macromolecular assemblies.

see Klaholz, *Open J. Statistics*, 2015.

Determining structures of multiple conformational states in a single sample

How to sort out heterogeneity?

→ particle sorting, advanced image processing

3 different approaches:

- 1) reference-based, i.e. cross correlation with forward-projections of known structures
- 2) multivariate statistical analysis (MSA): 2D classification or 3D classification
- 3) maximum likelihood based class assignment

Determining structures of multiple conformational states in a single sample

1) reference-based, i.e. cross correlation with forward-projections of known structures

"supervised classification":

**uses projections calculated from a known 3D template (i.e. external reference)
for comparison with particle images,
assign group according to best cross-correlation coefficients, i.e. projection matching**

if class membership and orientation parameters are estimated simultaneously:

***"unsupervised classification"* (K-means clustering, etc.)**

Practically:

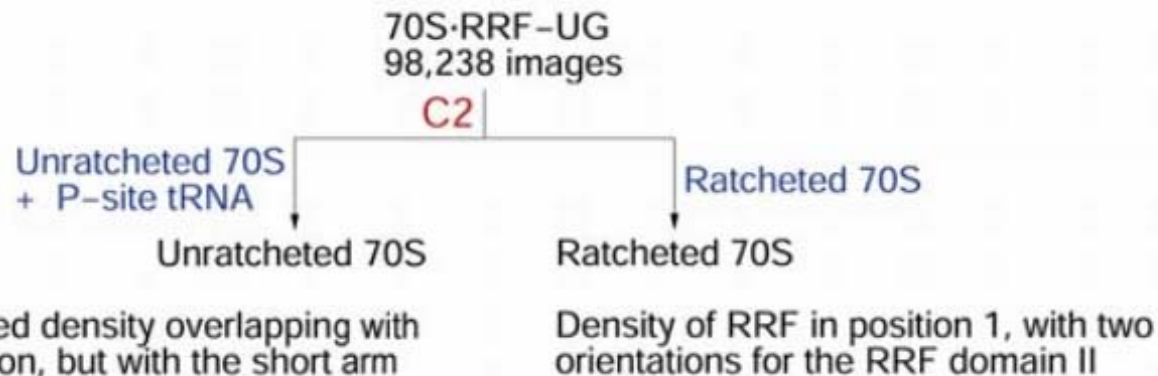
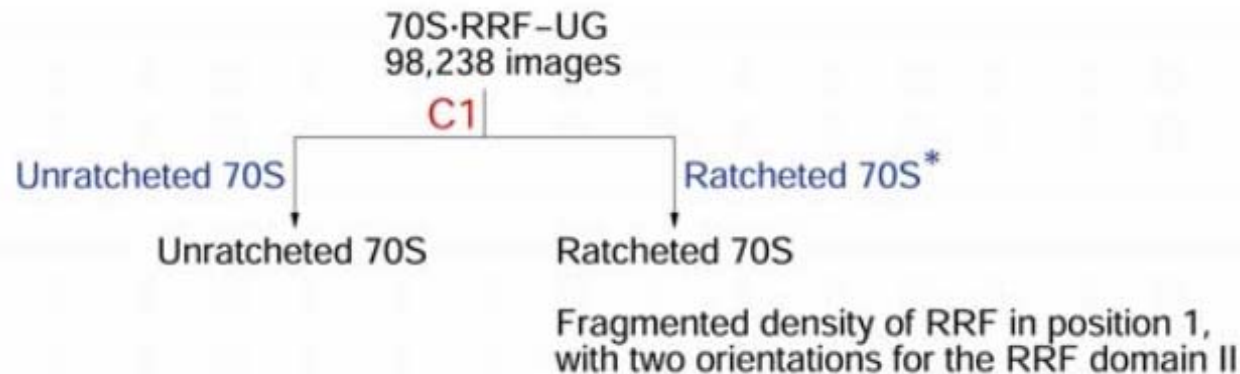
**use projections from several known 3D structures as references
(careful with the usage of crystal structures! use a strongly band-passed version),
run multi-reference alignment,
after a few cycles of refinement: add a reference (e.g. apo-form of a complex), iterate**

e.g. Gao *et al.*, 2004; Connell *et al.*, 2008; etc.

Determining structures of multiple conformational states in a single sample

1) reference-based, i.e. cross correlation with forward-projections of known structures

example 1:



A fragmented L-shaped density overlapping with the P-site tRNA position, but with the short arm of the L oriented in a diagonally opposite direction (RRF in position 2?)

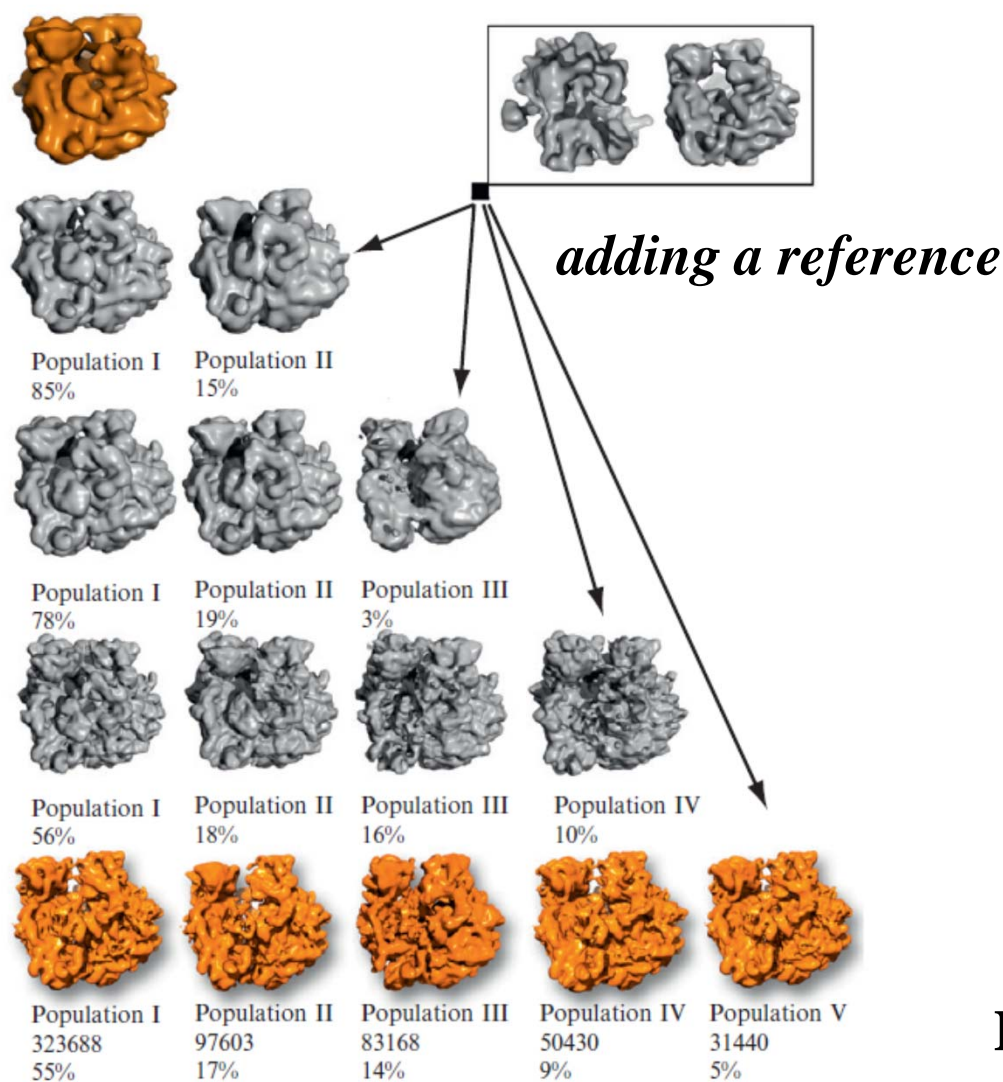
Density of the 30S subunit dramatically weaker than that of the 50S subunit

Barat *et al.*, *Mol. Cell* 2007.

Determining structures of multiple conformational states in a single sample

1) reference-based, i.e. cross correlation with forward-projections of known structures

example 2



Loerke *et al.*, *Meth. Enzymol.* 2010

Determining structures of multiple conformational states in a single sample

2) multivariate statistical analysis (MSA): 2D classification, 3D classification

Determining structures of multiple conformational states in a single sample

2) multivariate statistical analysis (MSA): 2D classification, 3D classification



distinguish: orientational classification and conformational classification

Determining structures of multiple conformational states in a single sample

2) multivariate statistical analysis (MSA): 2D classification, 3D classification



Emu, Pantanal, Brazil, 8.2014

front-view, conformation 2

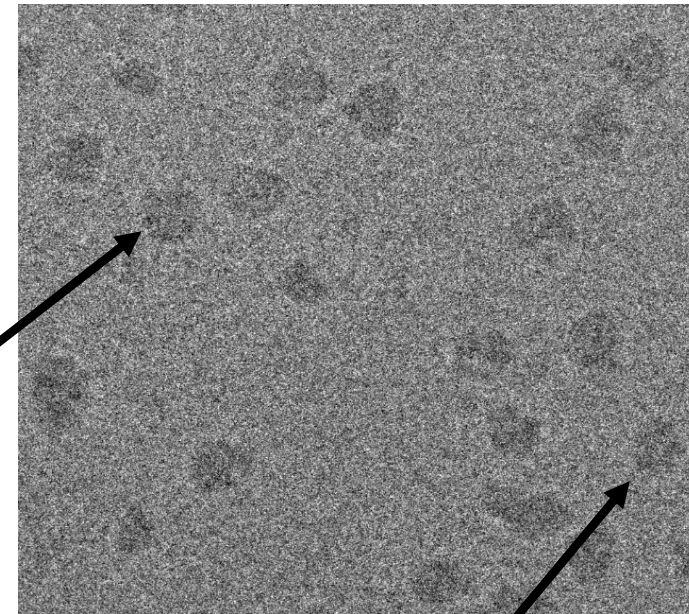
distinguish: orientational classification and conformational classification

Determining structures of multiple conformational states in a single sample

local 2D MSA (focused classification)



70S particle
without factors?



nom. defocus = 1

50S view of the 70S or 50S particle?

Perform 2 classifications:

- (i) global MSA for classification according to particle orientations (i.e. classical class averages),
- (ii) local MSA with a smaller mask for classification according to particle variability.

Klaholz *et al.*, *Nature* 2004; see Suppl. Mat.

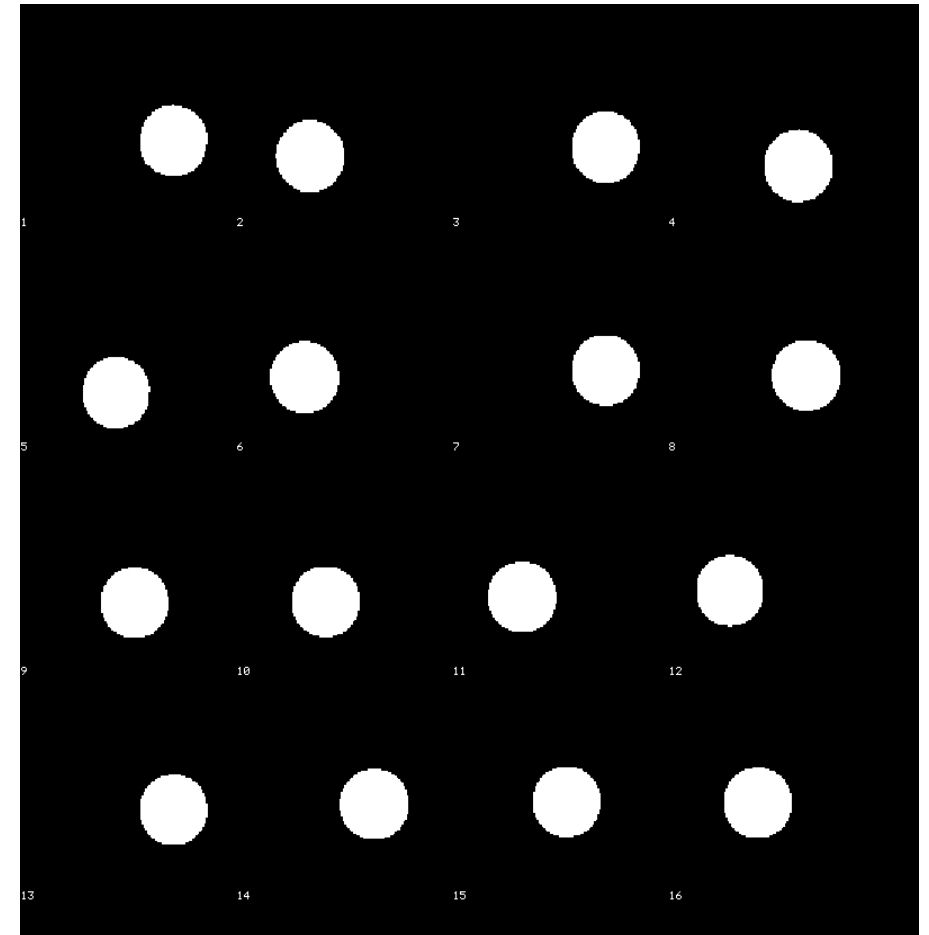
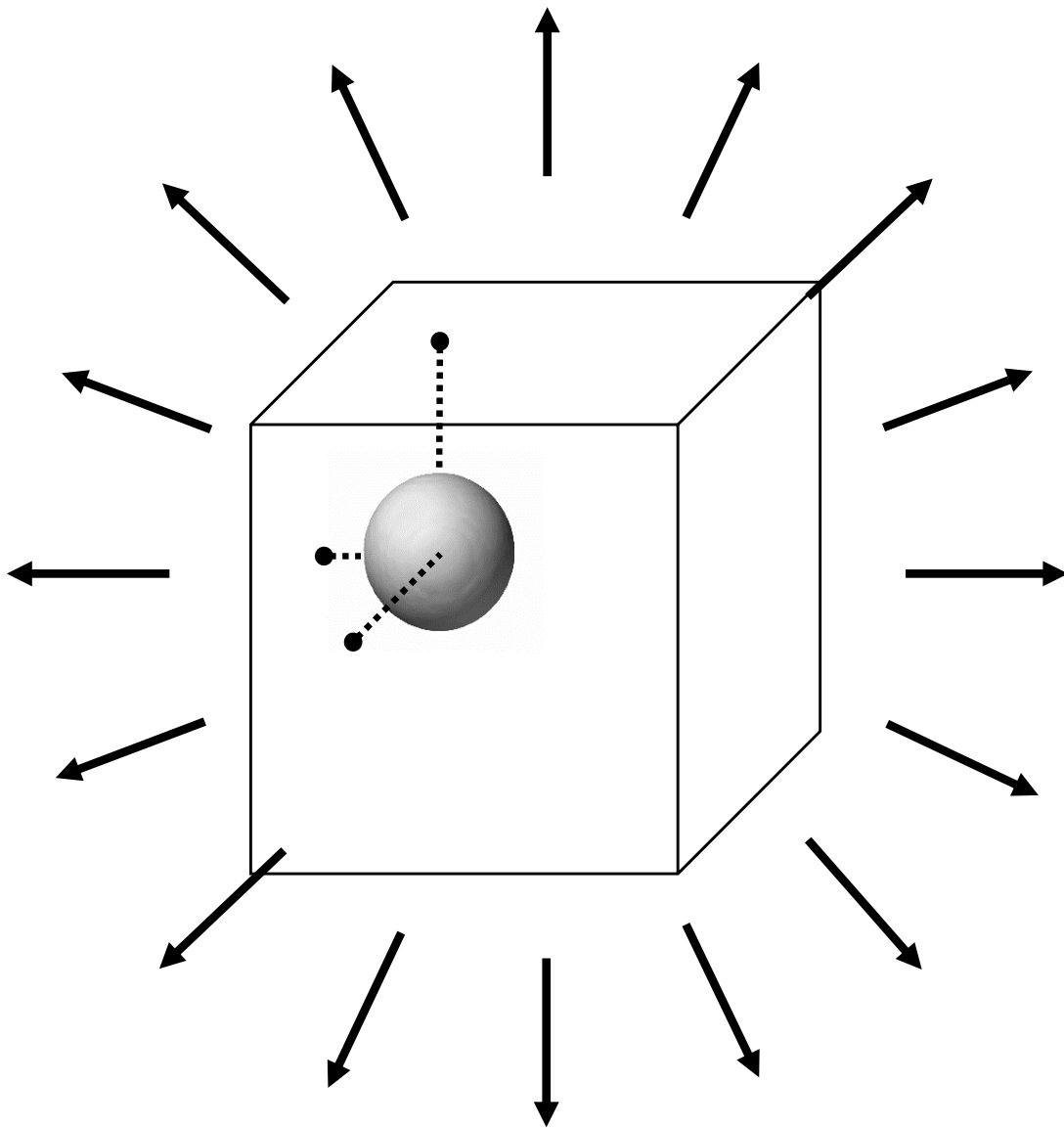
Determining structures of multiple conformational states in a single sample

Local / focused classification



Senard, France, 4.~2008-10

Determining structures of multiple conformational states in a single sample

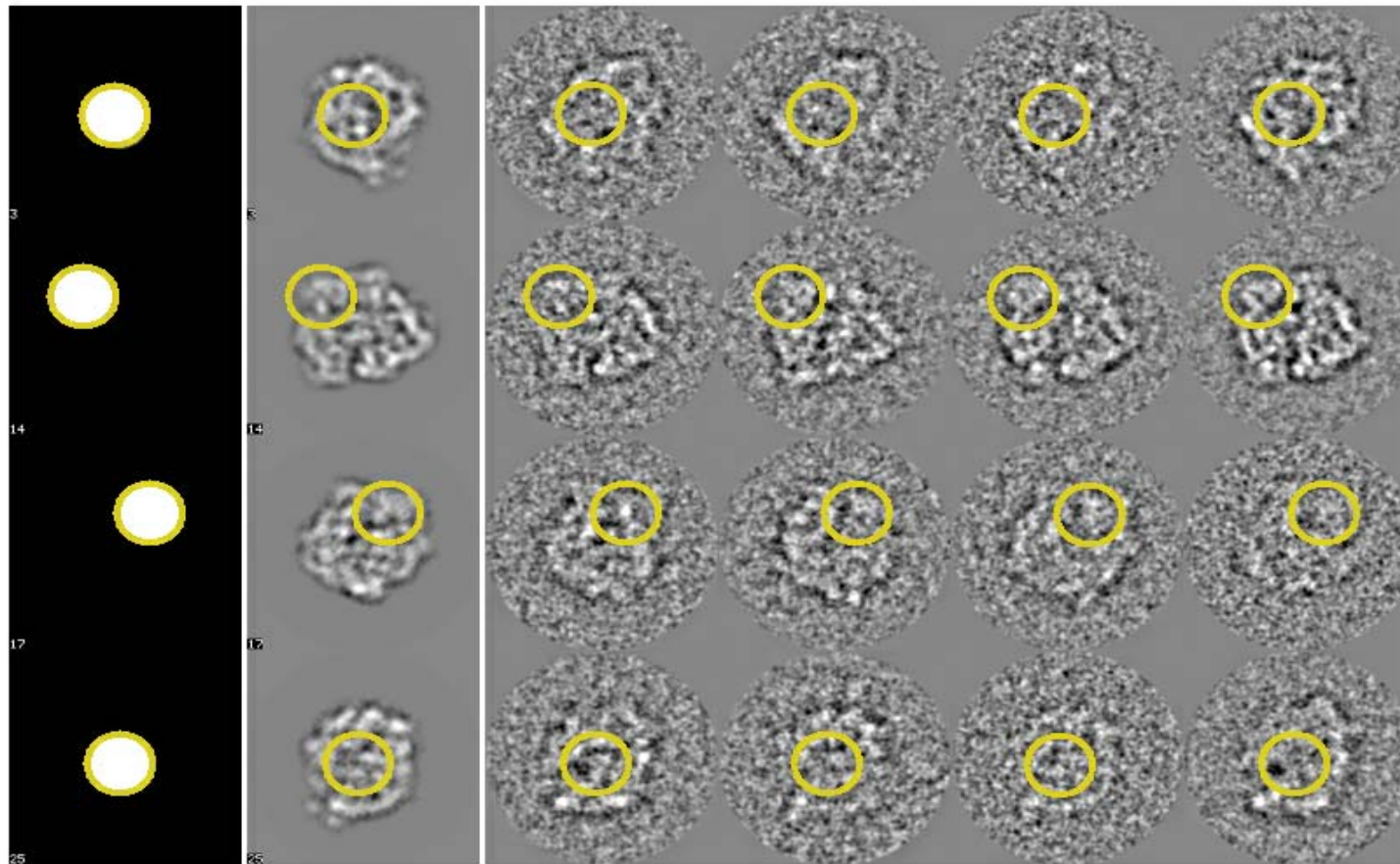


Klaholz, *Open J. Stat.* (2015).

Determining structures of multiple conformational states in a single sample

local 2D MSA

series of MSA's on particle views (class averages or extracted particles):

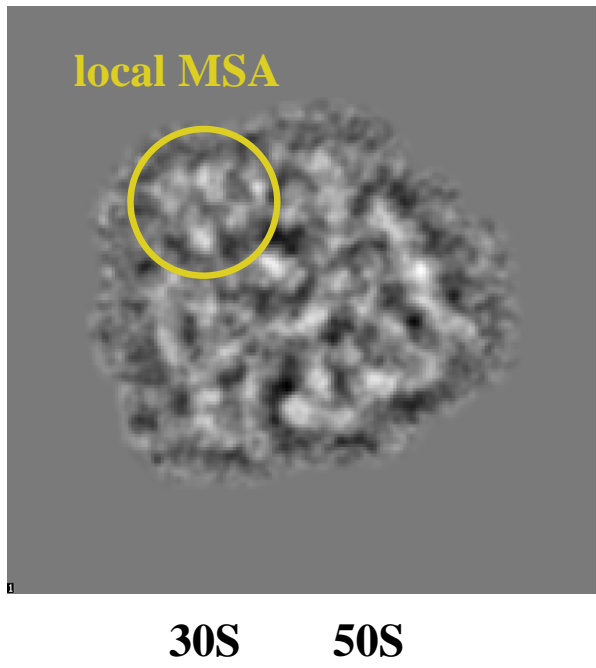


Klaholz *et al.*, *Nature* 2004; see Suppl. Mat.

→ allows re-classification after orientational classification

Determining structures of multiple conformational states in a single sample

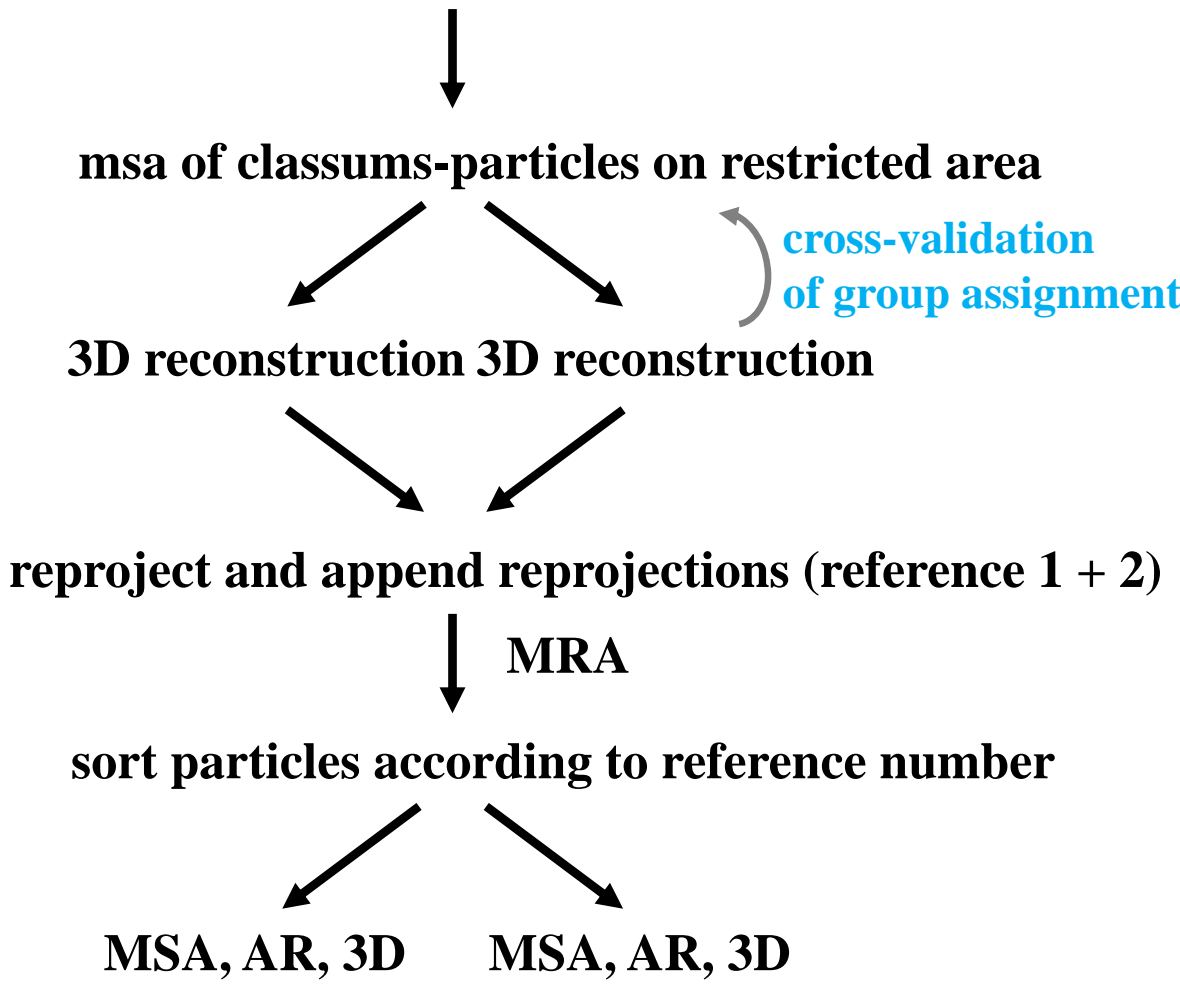
local 2D MSA



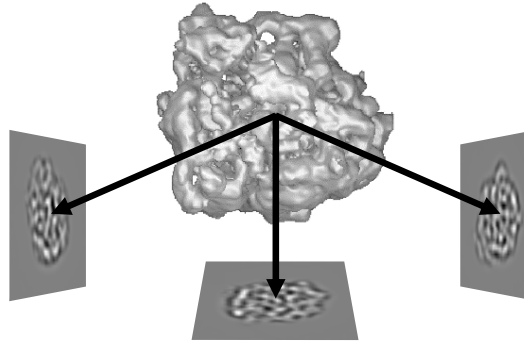
"seeding" with different structures,
from the sample (no external refs)

Image processing procedure

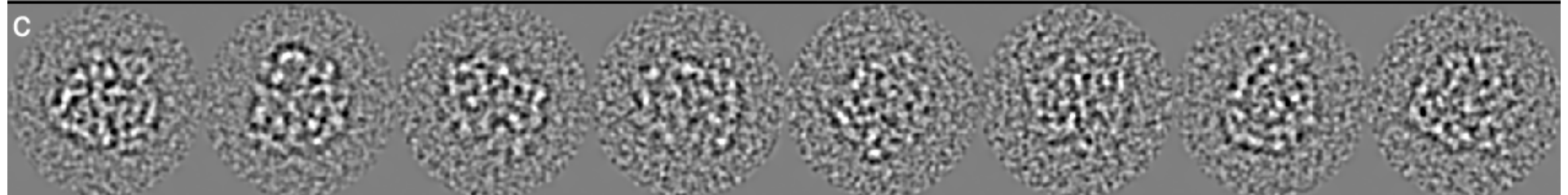
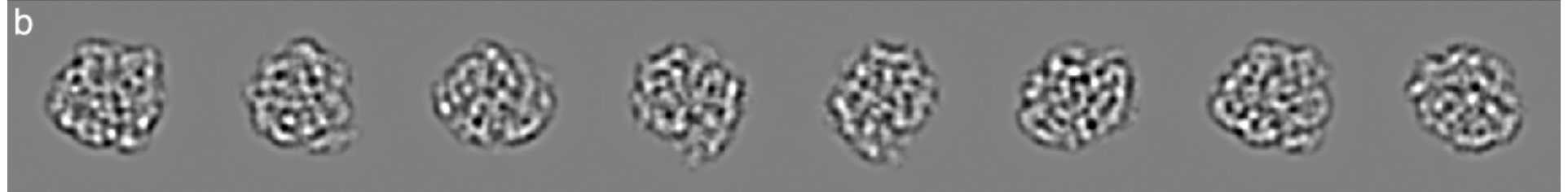
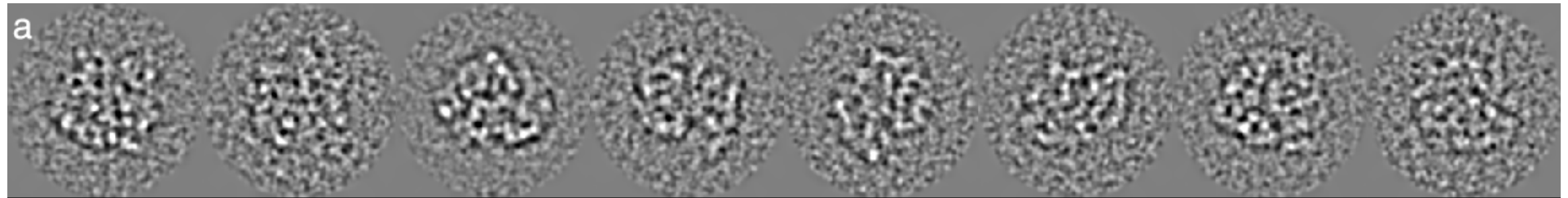
initial (merged) structure:
localise 3D area of disorder



group assignment by iterative cross-validation with corresponding re-projections



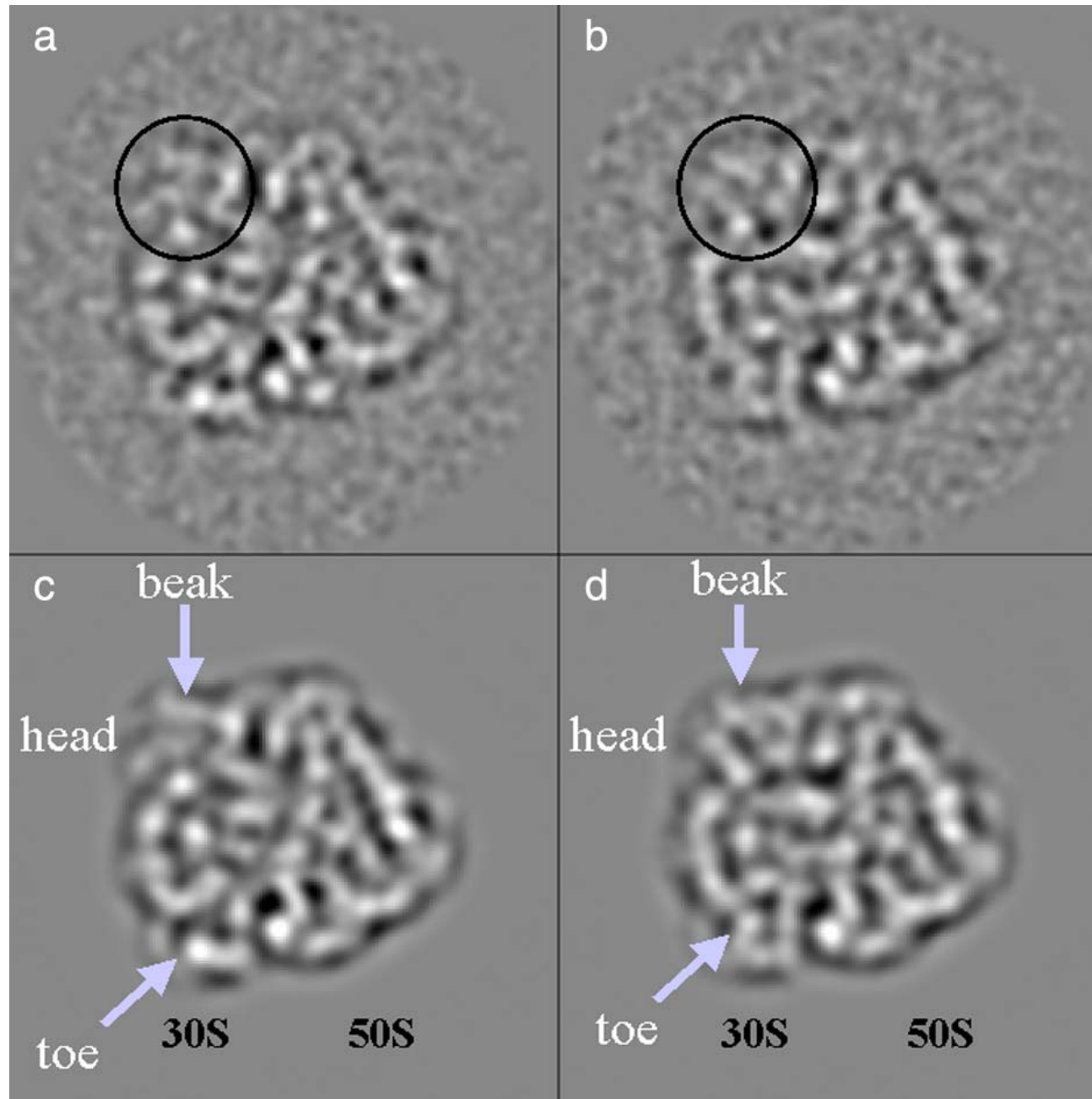
set 1



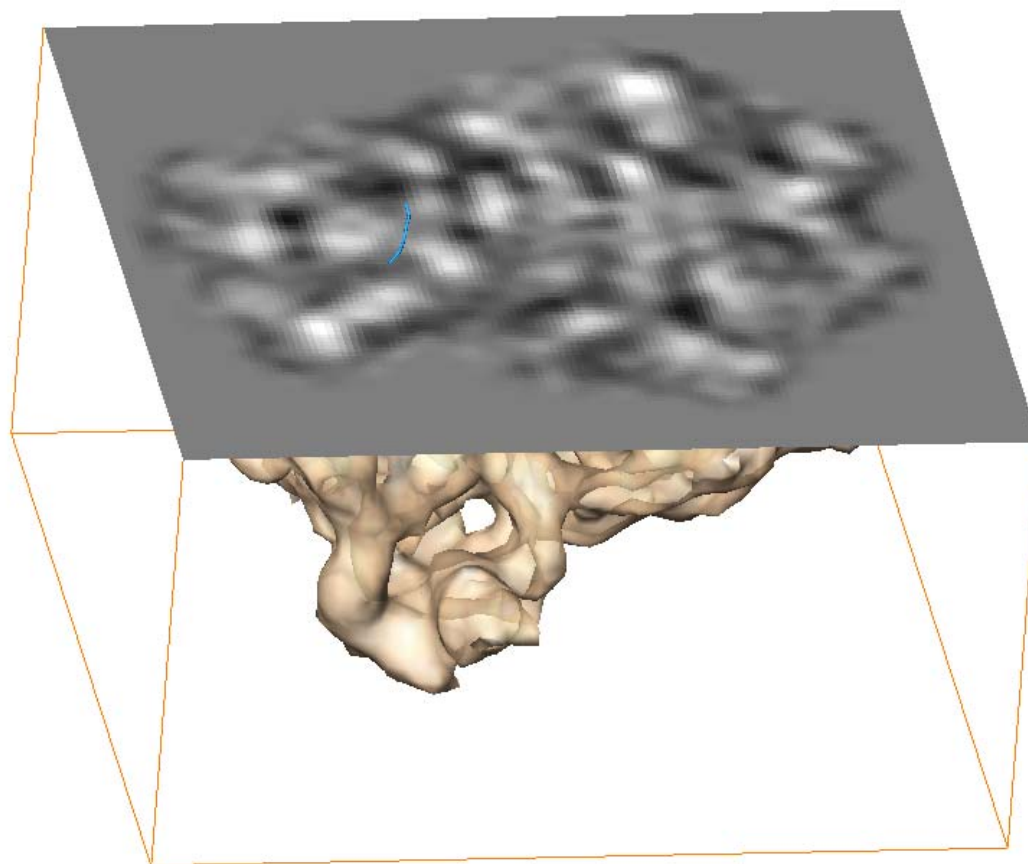
set 2

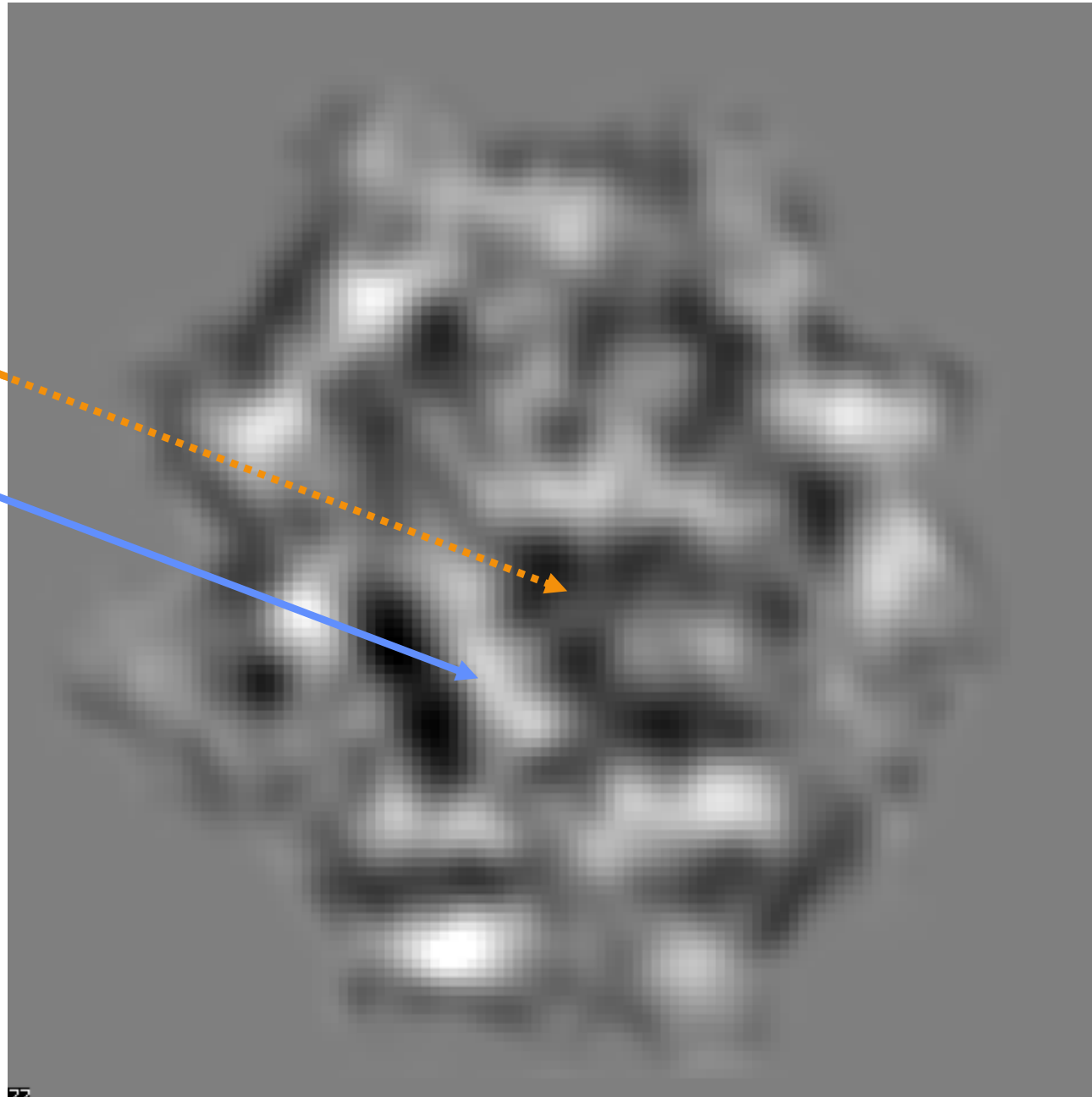


Procedure applied to distinct areas of the ribosome: conformational changes are correlated:



Sections through the 3D map:





P-site tRNA

E-site tRNA

Concept of
structure sorting
is true at 10-20 Å
resolution and
needs to be
validated at that
resolution,

but
also at 2 Å
resolution
(e.g. multiple
side-chain
conformations
seen in crystal
structures)

tRNA translocation

Intrinsic limitations of 2D-based particle sorting:

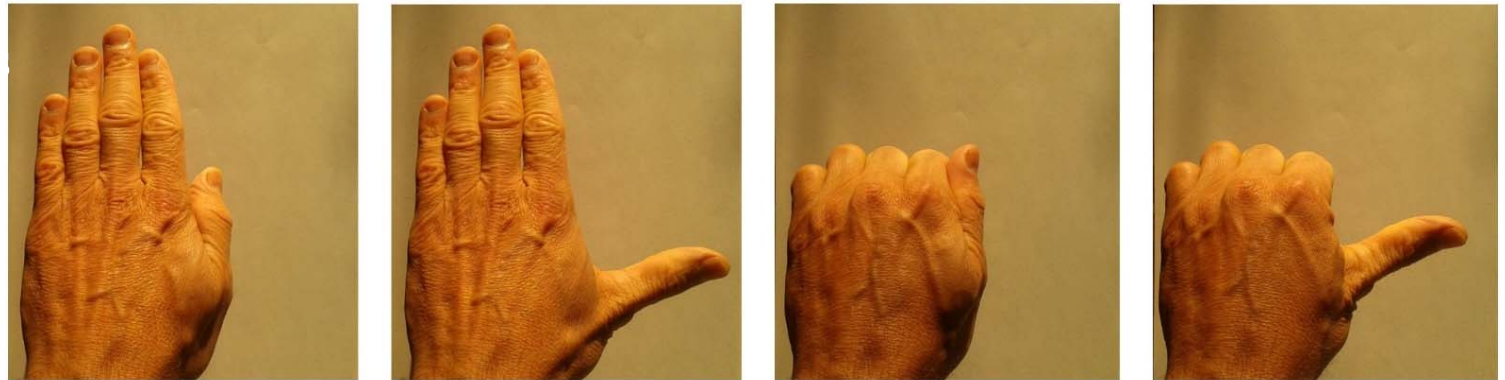
- (i) usually requires user-knowledge of the structure because some typical molecular views are needed to visually detect structural heterogeneity; solution: use variance map**
- (ii) it harbours the problem of assigning a particle image to a precise group (i.e. one structural state or another) across different viewing angles (addressed in part by automatic iteration of the cross-validation with re-projections);**
- (iii) the procedure is difficult to extend to more than two different states.**

MSA-based 3D classification

Determining structures of multiple conformational states in a single sample

Concept of 3D re-sampling and classification (3D-SC)

**different
conformations
of the 3D objects**



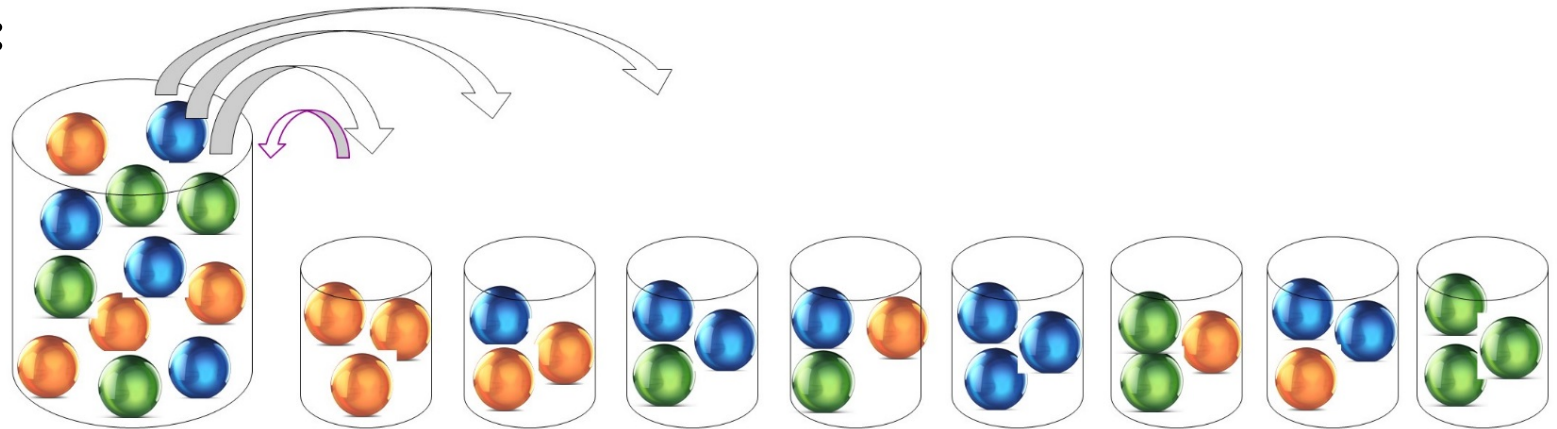
(here: conformational variability within a given orientation)

Determining structures of multiple conformational states in a single sample

Concept of 3D re-sampling and classification (3D-SC)

statistical resampling:

jack-knifing /
bootstrapping
("resampling")



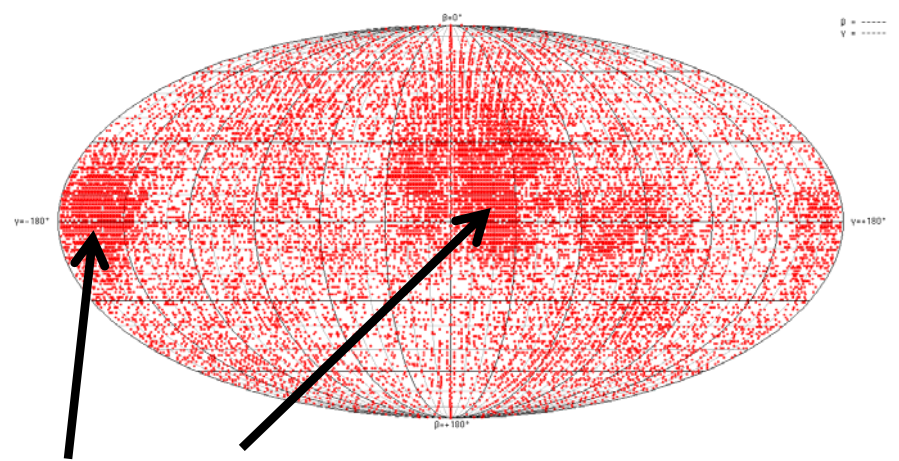
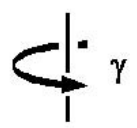
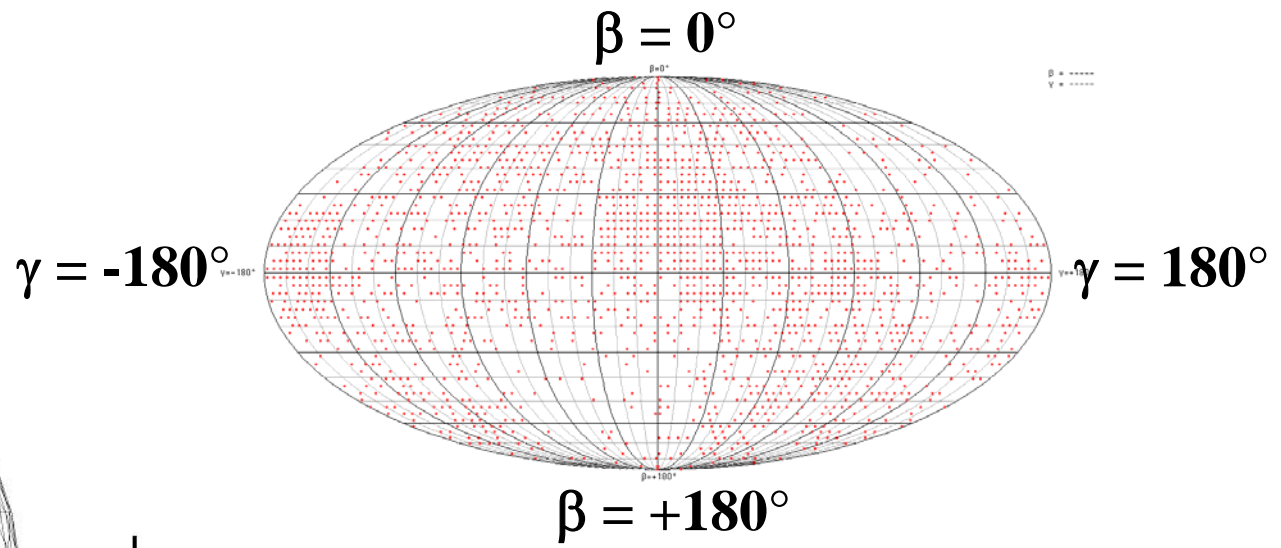
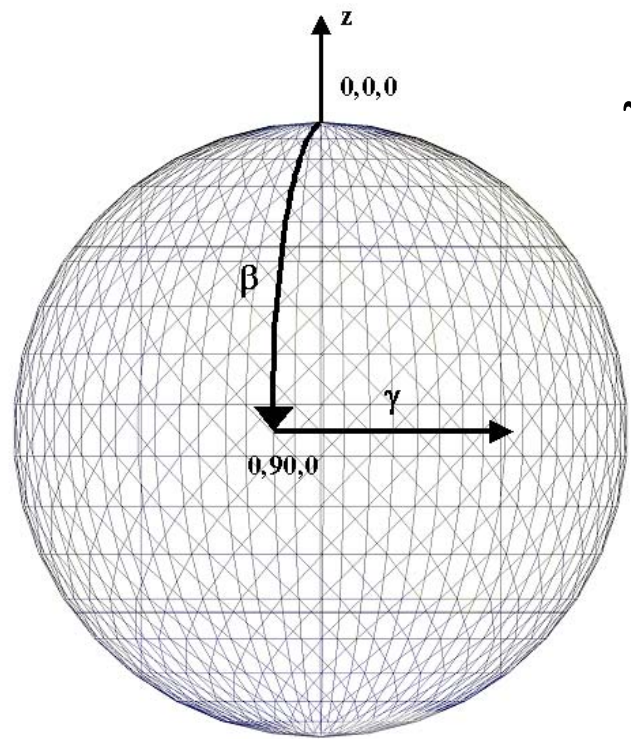
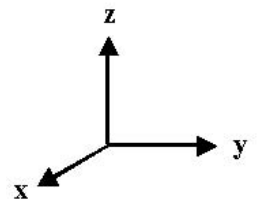
- **jack-knifing:** selection of small subsets
- **bootstrapping:** random selection of small subsets, part of which can be re-selected (resampling with replacement; repeated random resampling is a Monte Carlo approach)

see: [Quenouille, 1949](#); [Efron, 1979](#); [Simon, 1969 / 1997](#); [Good, 2005](#).

Determining structures of multiple conformational states in a single sample

3D MSA

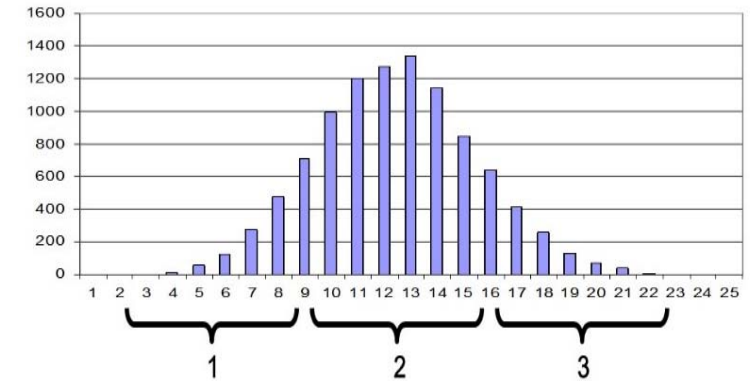
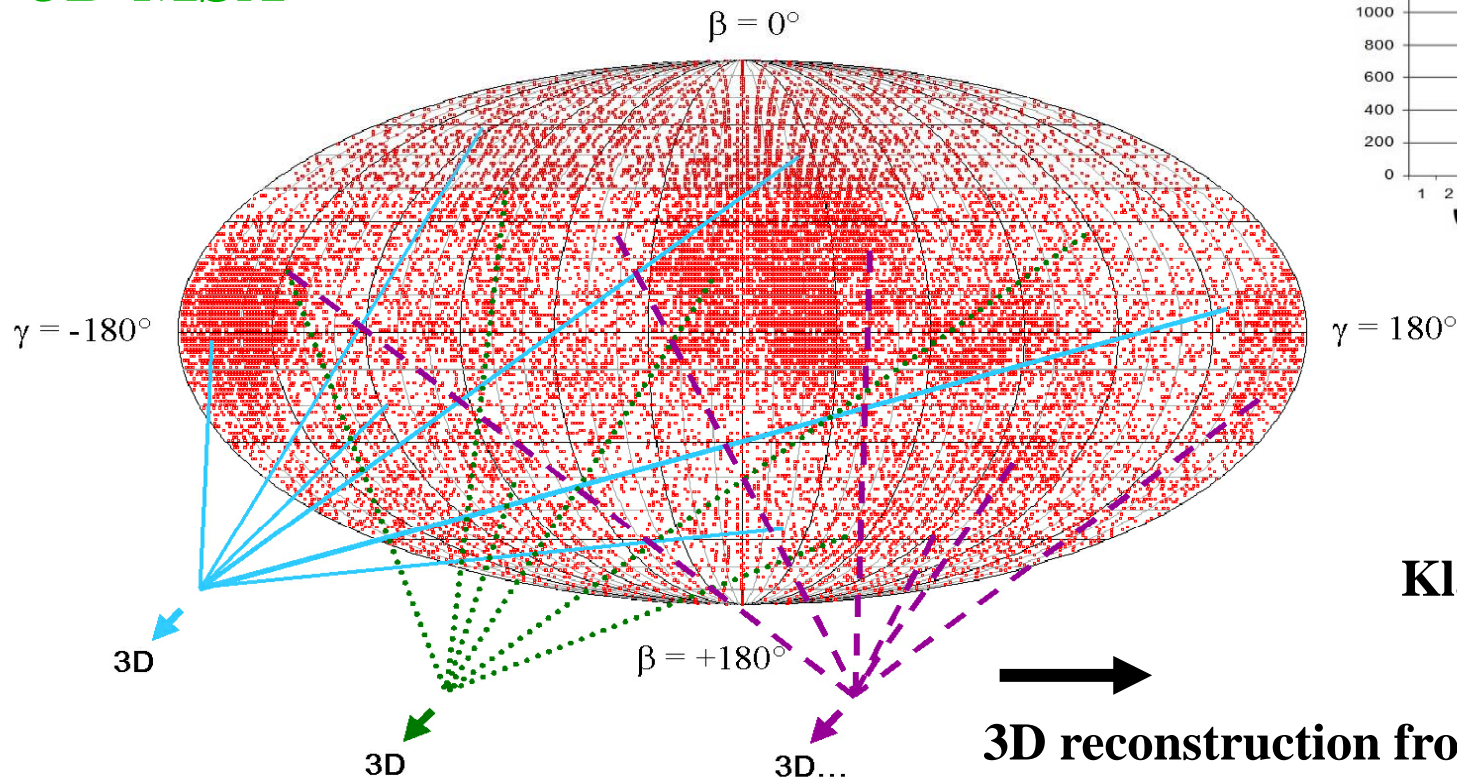
Particle angles plotted on sphere:



(preferential views)

Determining structures of multiple conformational states in a single sample

3D MSA



Klaholz, *Open J. Statistics*, 2015.

3D reconstruction from many subsets (resampling)
3D statistical analysis and 3D classification:
3D sampling and classification (3D-SC)

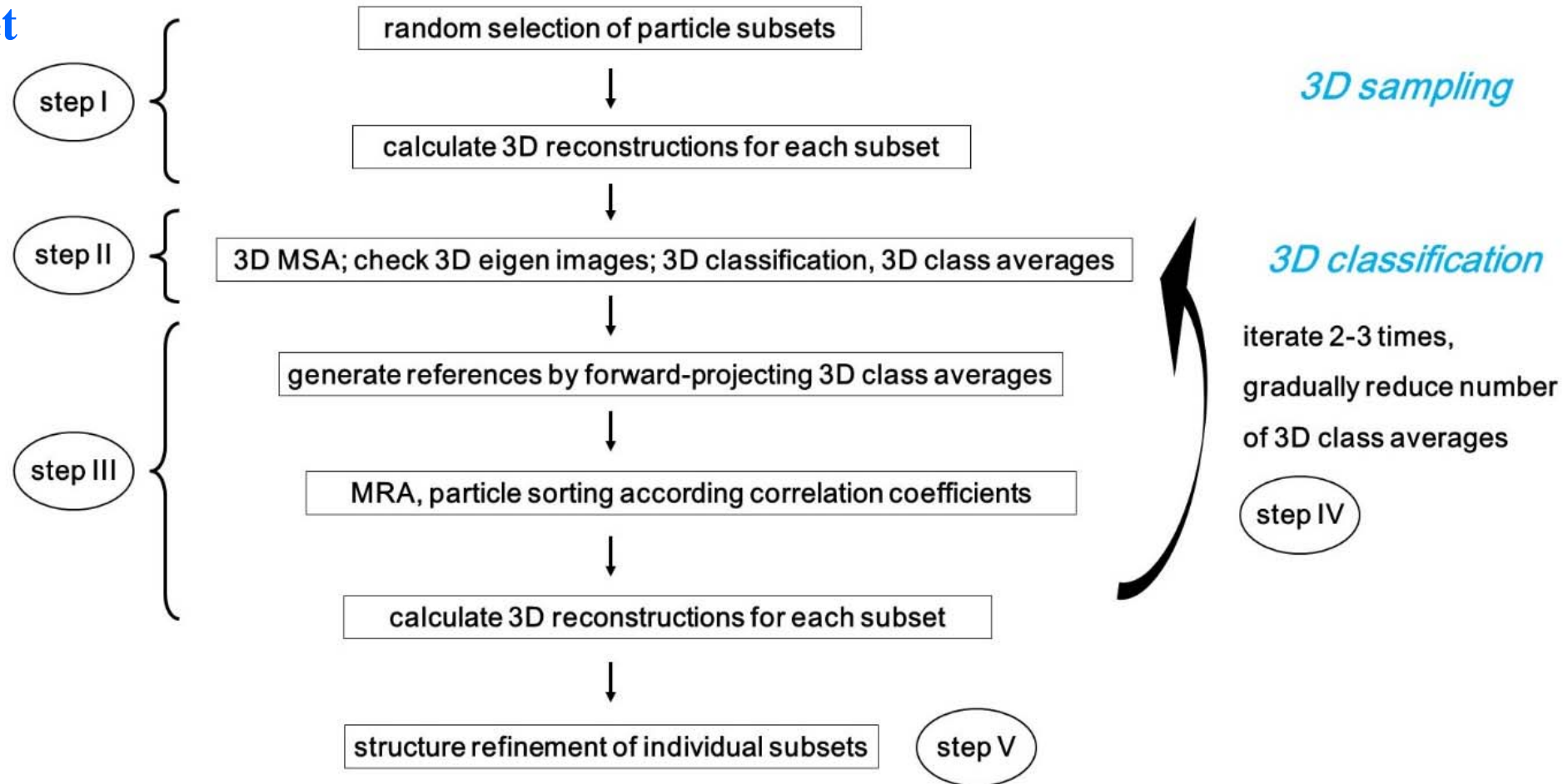
→ does both re-sampling and 3D classification, 3D variance map;
see also work by P. Penczek (bootstrapping (re-sampling), used primarily to find region of variance,
i.e. estimation of 3D variance)

Determining structures of multiple conformational states in a single sample

Concept of 3D sampling and classification (3D-SC)

**10-50
particles
per set**

e.g. per s
10 000
structures



initially use coarsened (binned) data to speed up the process

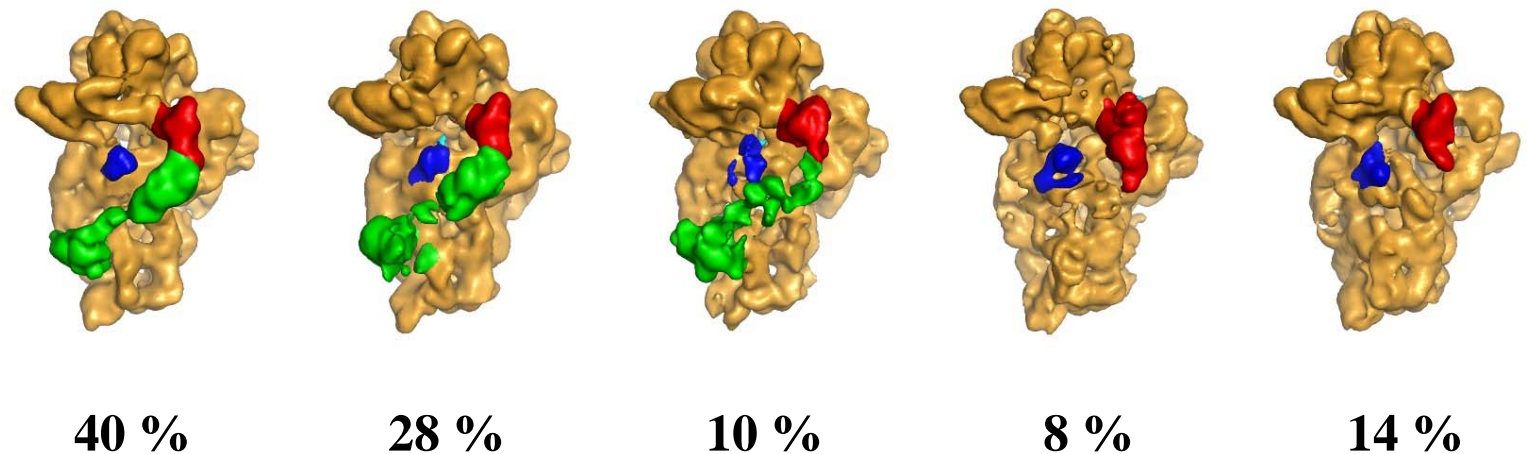
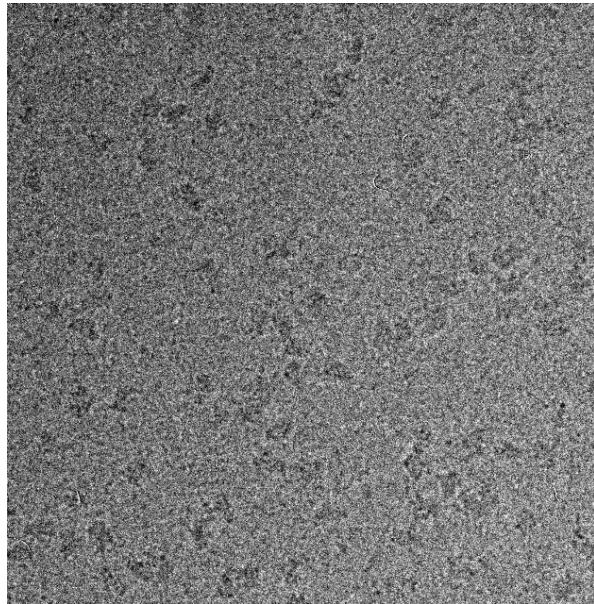
Klaholz, *Open J. Statistics*, 2015.

Determining structures of multiple conformational states in a single sample

3D MSA

3D reconstruction from many subsets (resampling),
3D statistical analysis and 3D classification:
3D sampling and classification (3D-SC)

Multiple states in the 30S initiation complex



no mRNA

Imagic

no IF2

200kV FEG data;

total 80 000 particles

resolution of 3D's: 9Å

2D → *3D* → *4D*

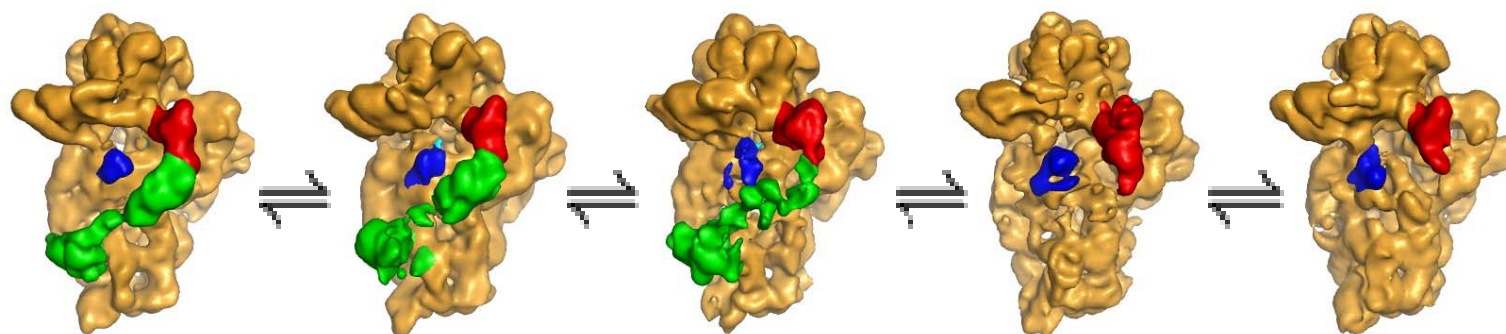
Simonetti *et al.*, *Nature*, 2008.

Determining structures of multiple conformational states in a single sample

3D MSA

Addressing the structural state of reaction intermediates
that are in equilibrium with each other!

particle populations

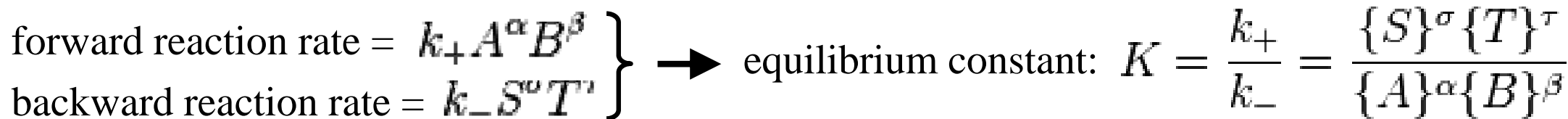


28 %

10 %

8 %

14 %

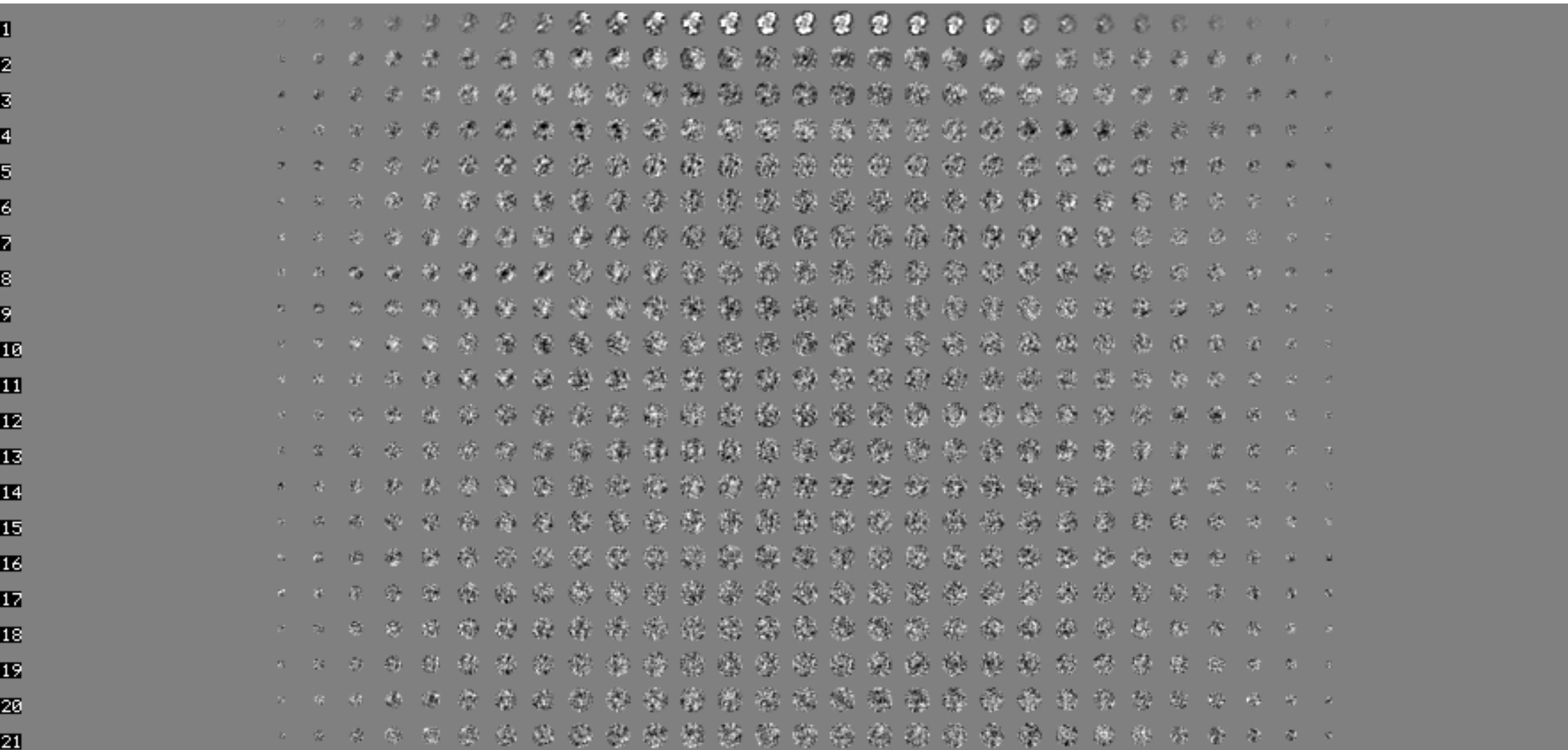


The 3D classification procedure 3D-SC has been used since by other groups also:
(Papai *et al.*, *Nature* 2010; Fischer *et al.*, *Nature* 2010).

Simonetti *et al.*, *Nature*, 2008.

3D MSA

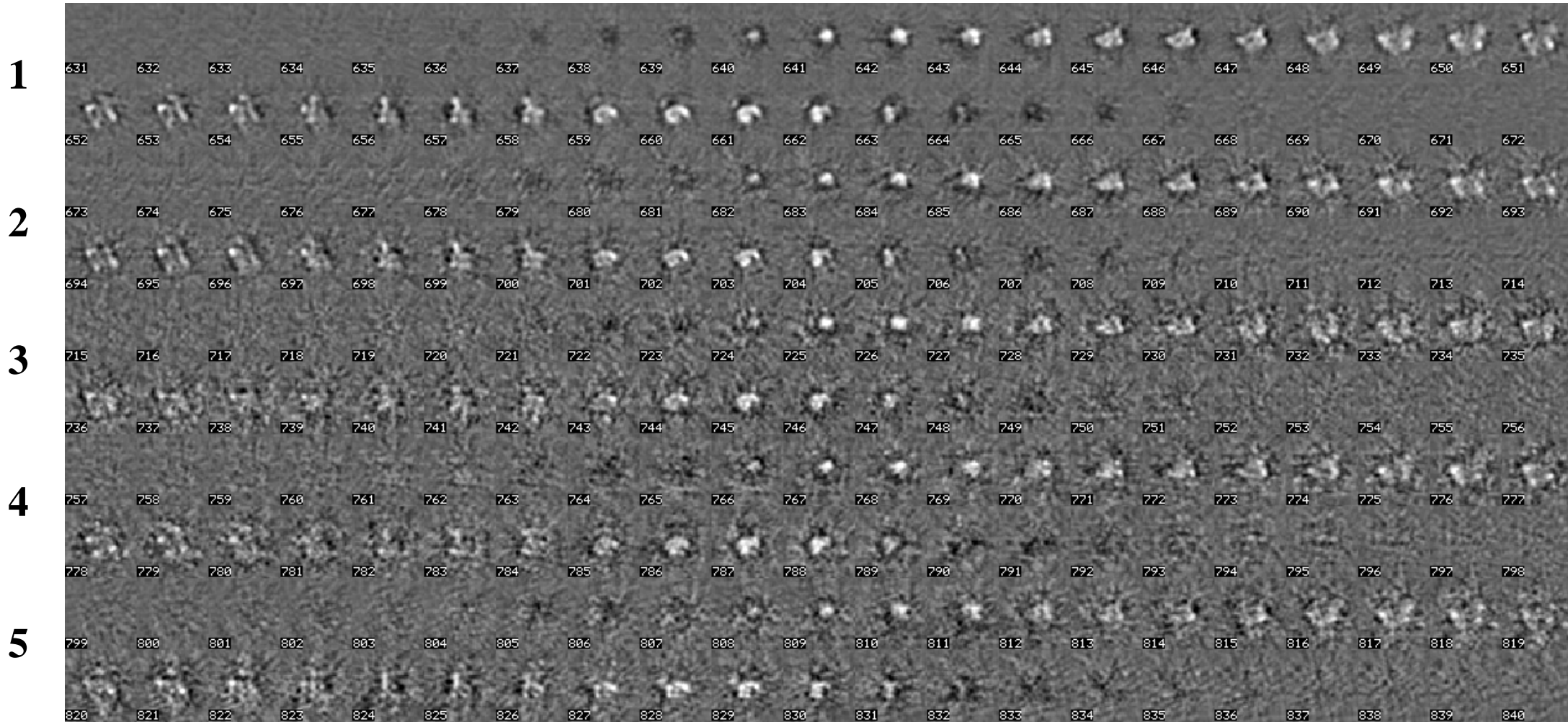
3D eigenimages: (30S)



Klaholz, *Open J. Statistics*, 2015.

3D MSA

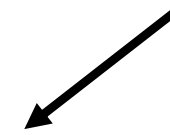
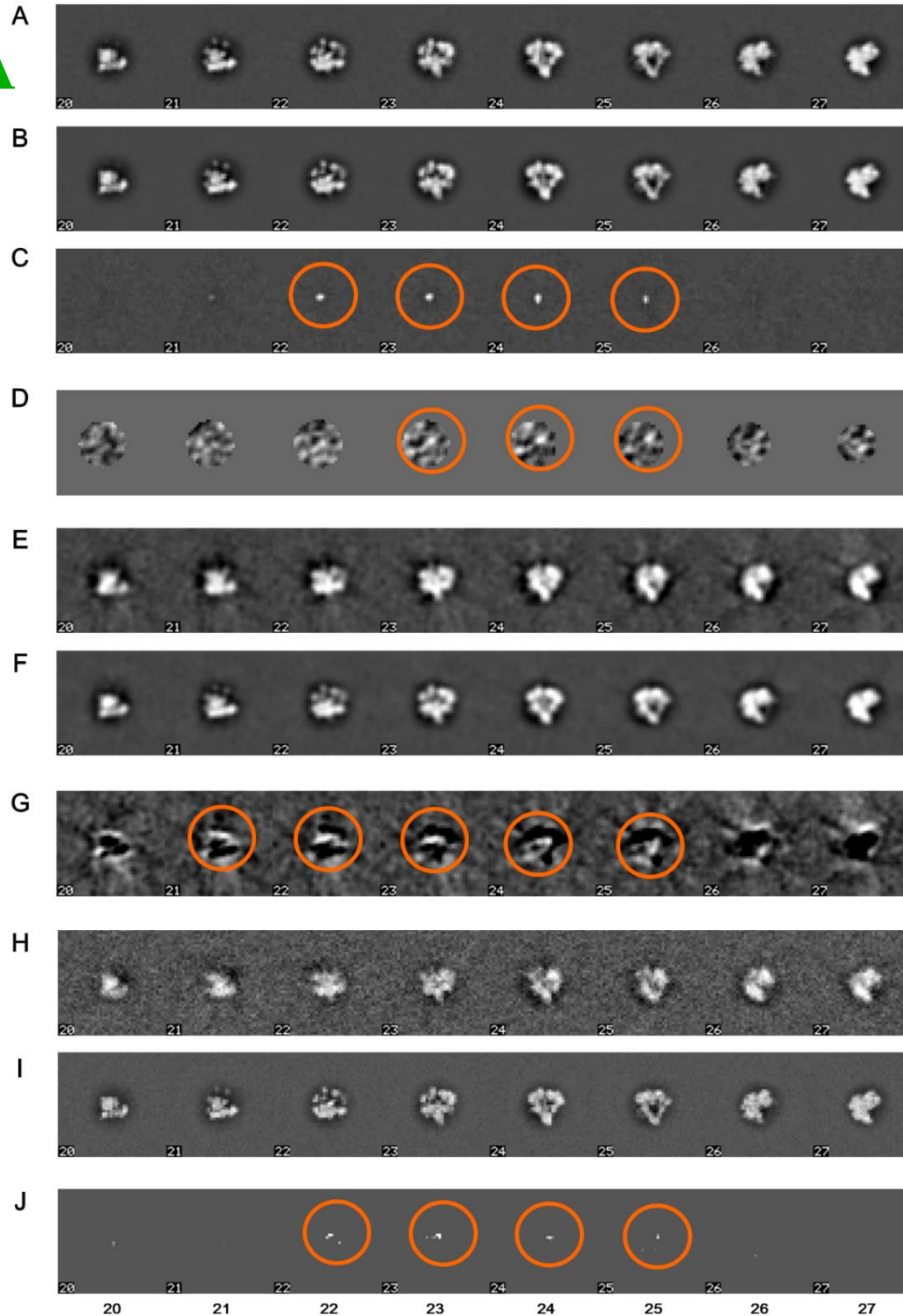
3D class averages: (30S)



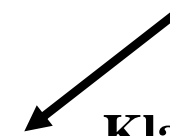
3D #

Klaholz, *Open J. Statistics*, 2015.

3D MSA



small difference found by 3D MSA
($<1\%$ of the total mass
of the complex;
modeled RNA Pol data)



Klaholz, *Open J. Statistics*, 2015.

Imagic

Some examples based on 2D classification or on 3D classification (3D-SC / resampling / bootstrapping):

Klaholz *et al.*, 2004; White *et al.*, 2004 (size variation);

Penczek *et al.*, 2006; Cheng *et al.*, 2007;

Elad *et al.*, 2008; Simonetti *et al.*, 2008;

Wang *et al.*, 2013;

Liao *et al.*, 2015.

focused classification / focused refinement:

concept implemented later into Relion, FREALIGN etc.

→ analyse regions, subunit structural variations

→ not limited by the number of different structural states in the sample

Determining structures of multiple conformational states in a single sample

3) maximum likelihood based class assignment

→ assign particles to different 3D classes based on maximum likelihood (max. expectation)
(probability distribution; uses randomly selected references + ML-weighting)

Practically:

random subsets are optimized and a low-resolution average structure is used as reference,
i.e. resampling is used in combination with likelihood optimization

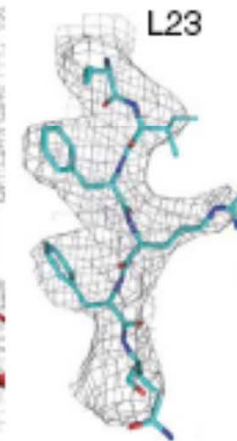
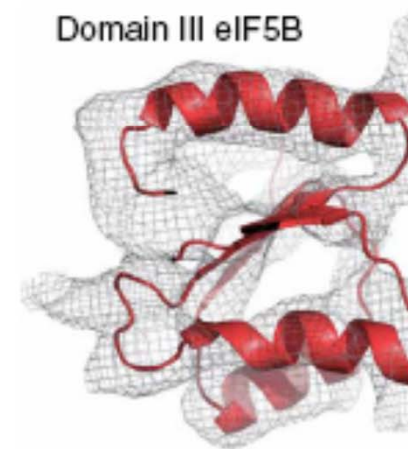
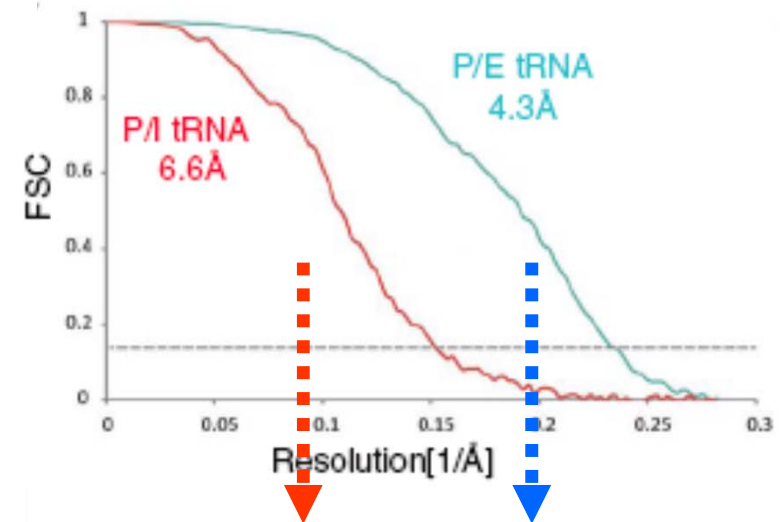
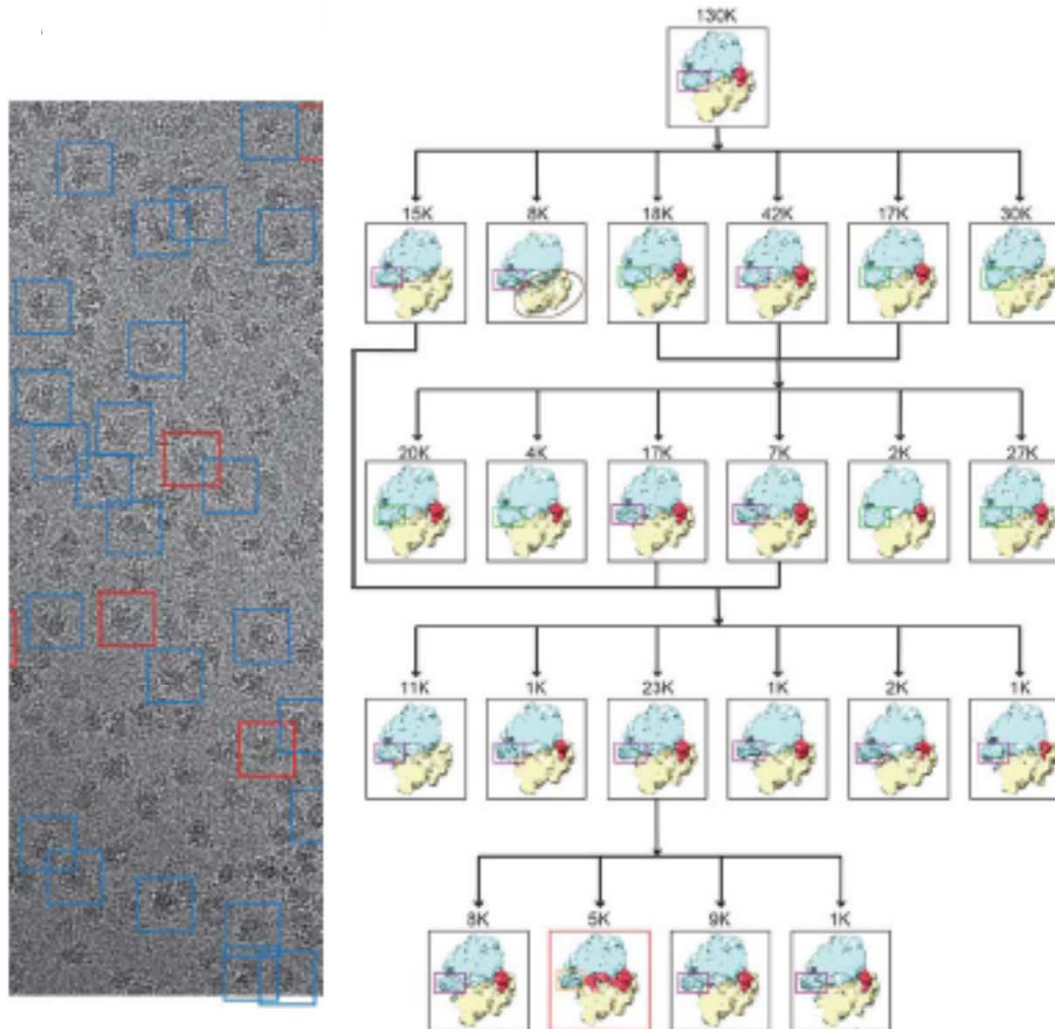
e.g. Scheres *et al.*, *JMB* 2005; *Meth. Enzymol.* 2010;

Lyumkis *et al.*, *JSB* 2013

Introduction of the ML concept in cryo-EM: Sigworth, *JSB* 1998;

in X-ray crystallography: G. Bricogne, *Acta Cryst A*, 1991.

Examples of ML-based 3D classification

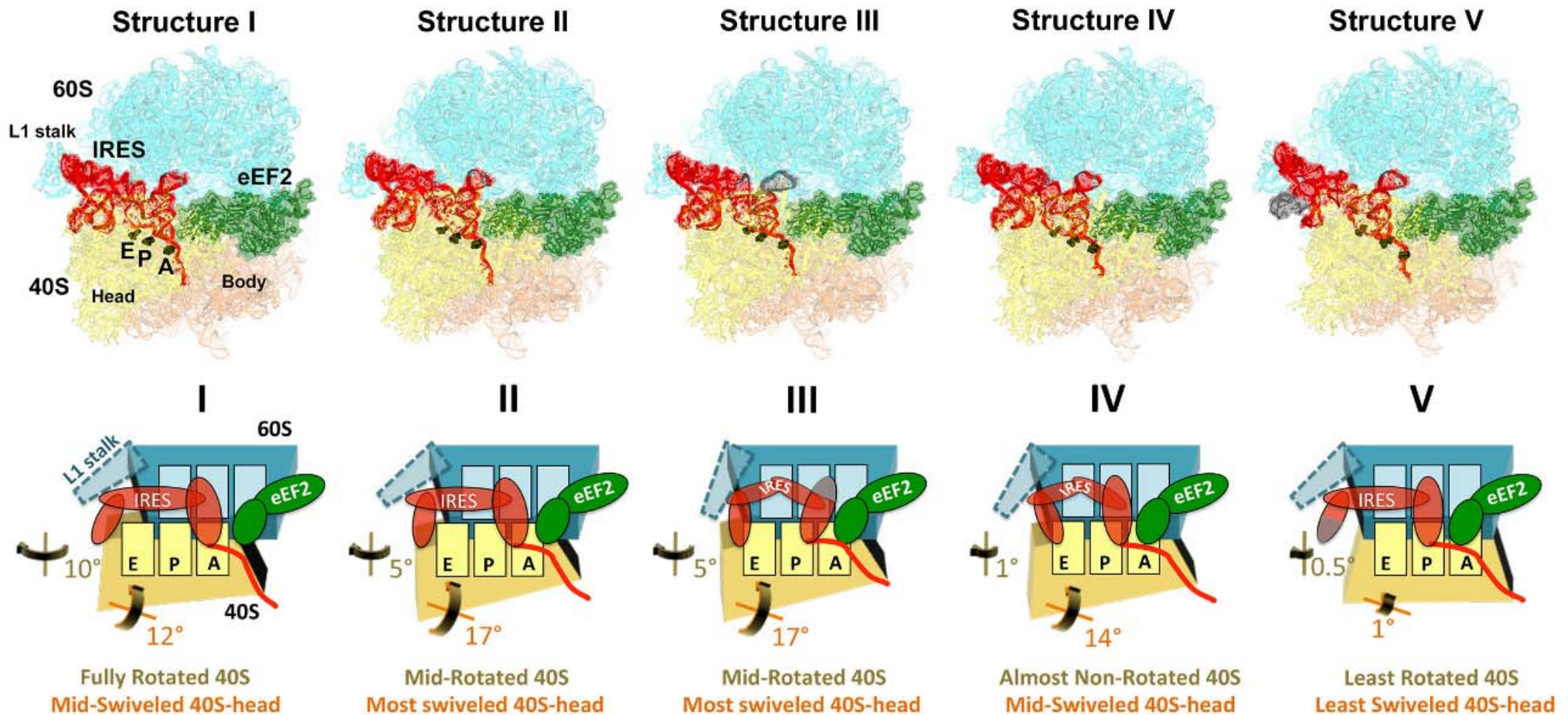


5 000 **40 000 particles**

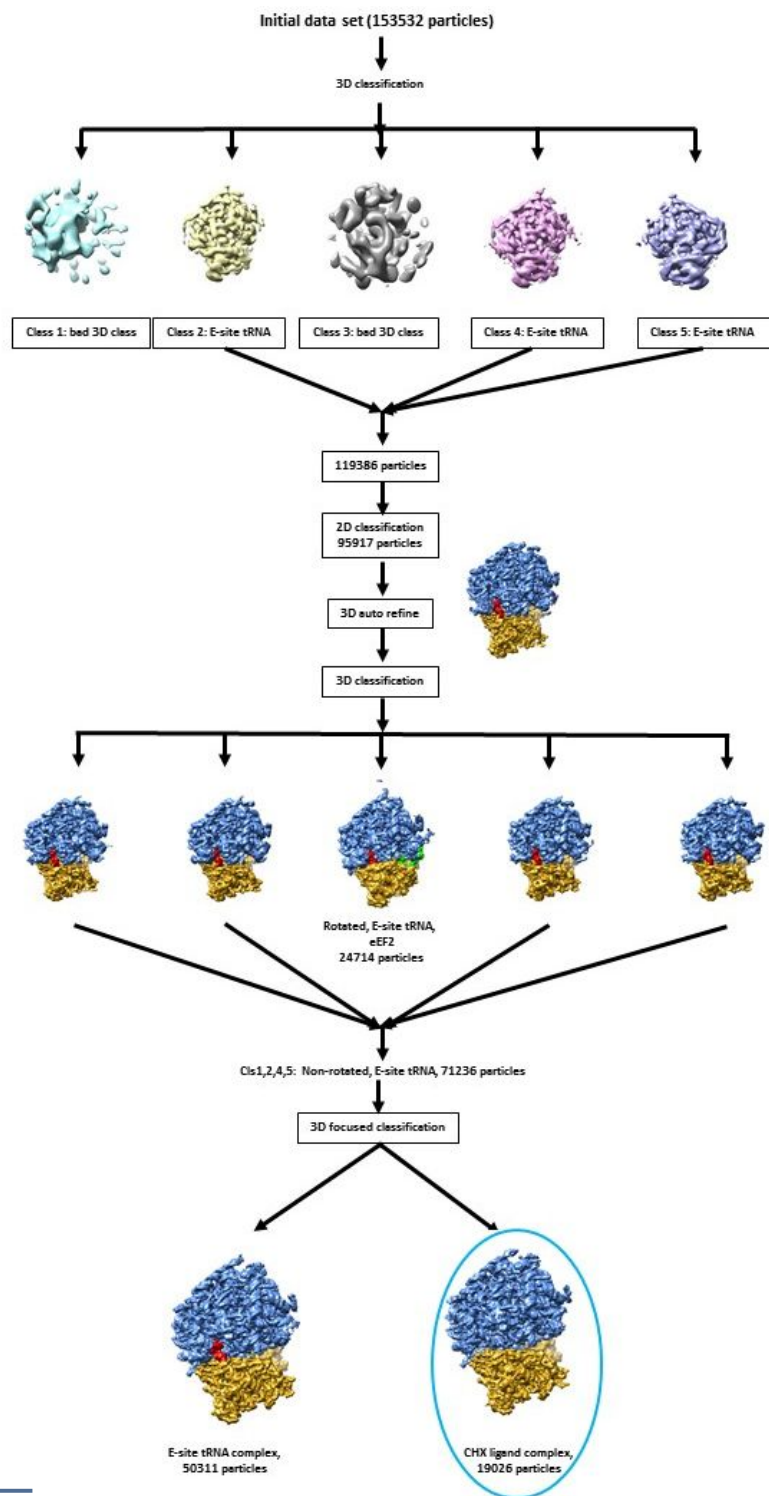
Strong heterogeneity of a reconstituted eukaryotic translation initiation (eIF5B) complex:
sorting → 5143 particles, representing 3% of the population in the sample, 6.6 Å reconstruction.

Fernández *et al.*, *Science* 2013; V. Ramakrishnan & S. Scheres.

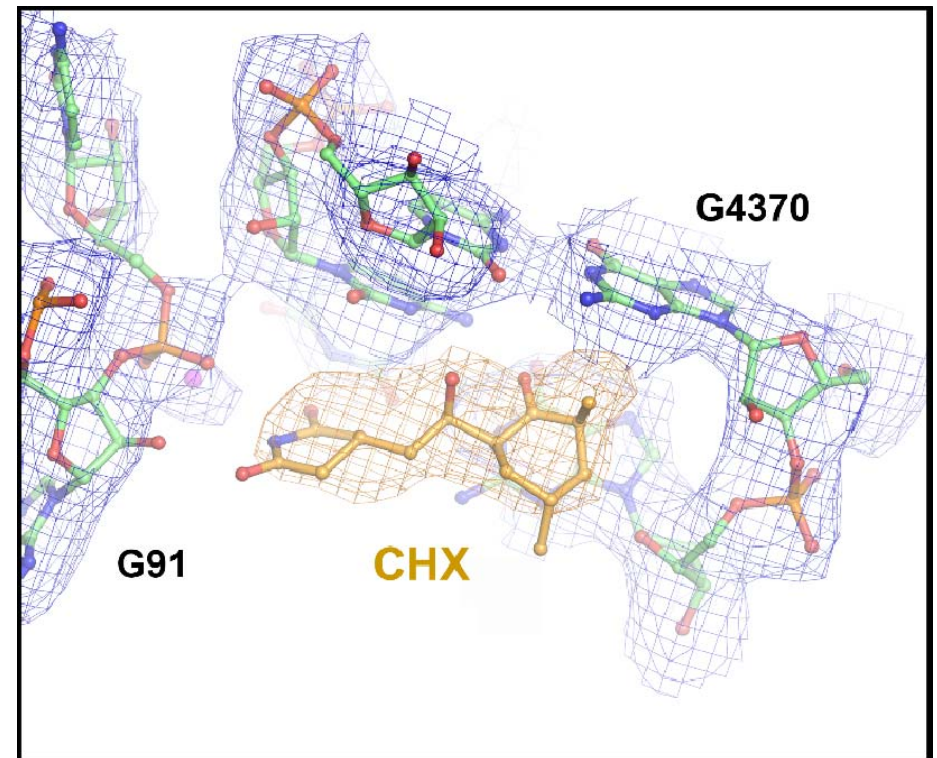
e.g. ML-based focused classification
of 80S / TSV IRES complex with eEF2/GDP/sordarin



Abeyrathne *et al.*, *eLife* 2016



e.g. ML-based focused classification
sorting scheme for human 80S/antibiotic complex



Myasnikov *et al.*, *Nat. Comm.* 2016.

Summary:

Determining structures of multiple conformational states in a single sample

Possibilities to address heterogeneity:

- 1) reference-based, i.e. cross correlation with forward-projections of known structures**
- 2) multivariate statistical analysis (MSA): 2D classification or 3D classification
variance analysis + resampling, bootstrapping, 3D resampling**
- 3) maximum likelihood based class assignment**
- 4) deep learning methods (coming)**

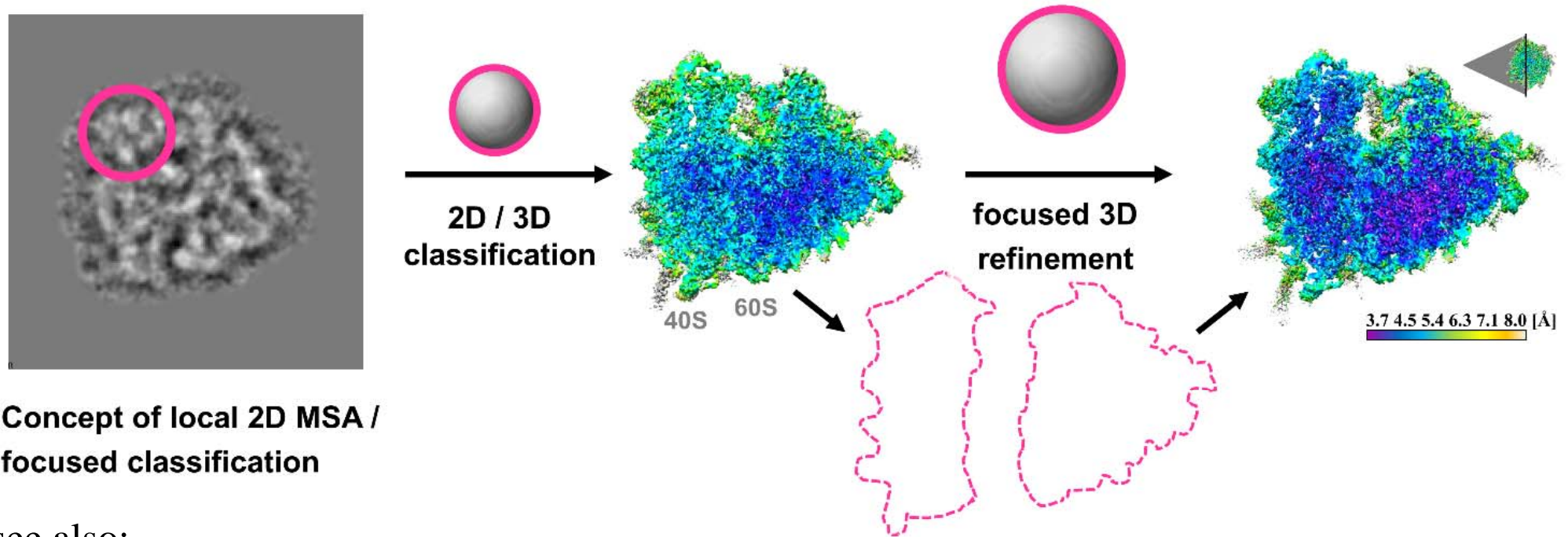
Summary:

Determining structures of multiple conformational states in a single sample

Conclusions & tips:

- **do not assume a single state in your sample / multi-subunit complex**
- **consider lower symmetry (viruses etc.) to see differences between subunits**
- **if to use local / focused classification/refinement: use slightly larger region**
- **also useful in sub-tomogram averaging and 3D classifications**
- **consider: any sub-ensembles will not be entirely homogeneous due to the statistical nature of the procedures (resampling and/or ML)**
- **after 3D classification: go for focused refinement →**

Local MSA / focused 2D/3D classification & focused refinement:



see also:

Klaholz *et al.*, *Nature* 2004;

White *et al.*, *JSB* 2004;

Penczek *et al.*, *JSB* 2006;

Wong *et al.*, *Elife* 2014;

...

Concept of focused cryo-EM structure refinement through

- 3D resampling & 3D classification (3D-SC) / bootstrapping

- maximum likelihood 3D classification

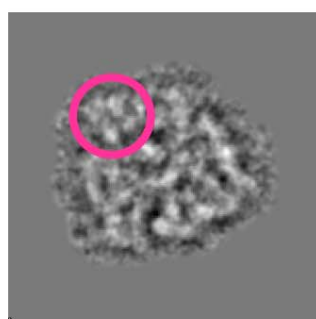
using spherical mask or dilated, binarized map of region of interest

Helps: use a slightly larger region than the region of interest, e.g. 30-50 Å in diameter

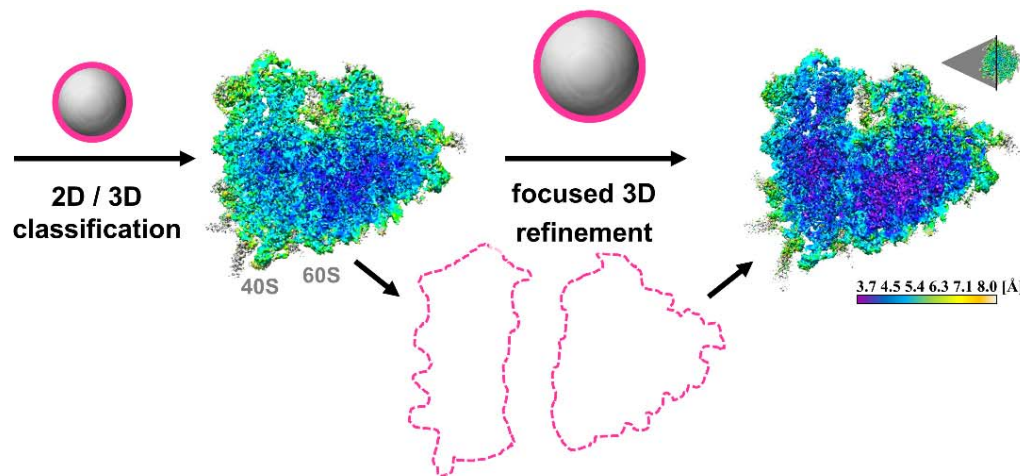
von Loeffelholz *et al.*,
Curr. Opin. Struct. Biol. 2017.

Advanced image processing to improve cryo-EM reconstructions and map interpretation

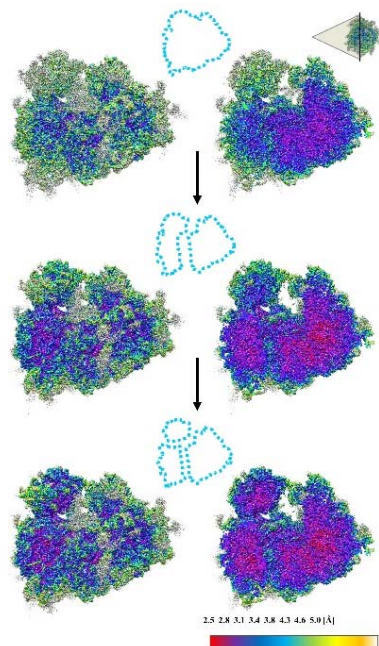
Local MSA / focused 2D/3D classification & focused refinement:



Concept of local 2D MSA /
focused classification
Klaholz *et al.*, 2004.



von Loeffelholz *et al.*,
Curr. Opin. Struct. Biol. 2017.

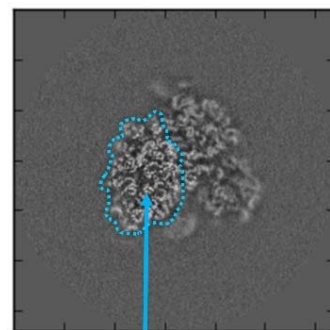


Focused refinement

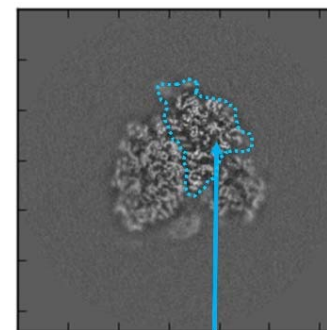
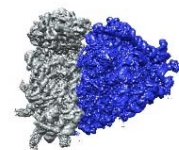
global 80S refinement

refinement of the individual
60S and 40S ribosomal subunits

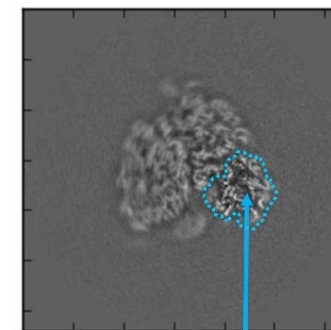
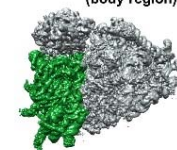
refinement of the individual
60S subunit, 40S body and 40S head regions



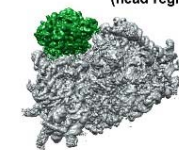
human 60S ribosomal subunit



human 40S ribosomal subunit
(body region)

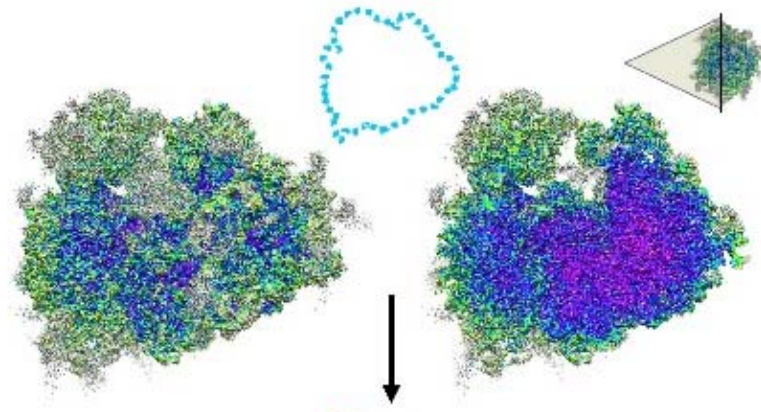


human 40S ribosomal subunit
(head region)

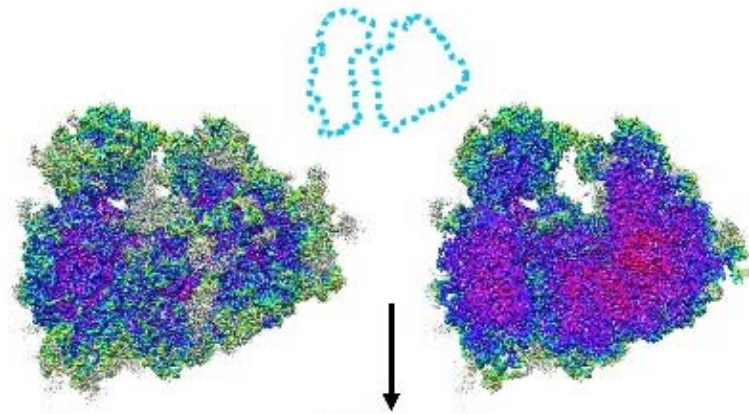


Natchiar *et al.*, *Nature* 2017.

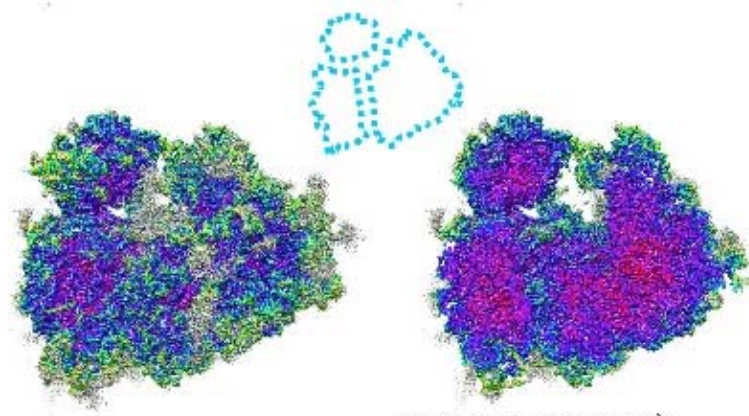
Focused refinement (with subtraction, Relion)



global 80S refinement

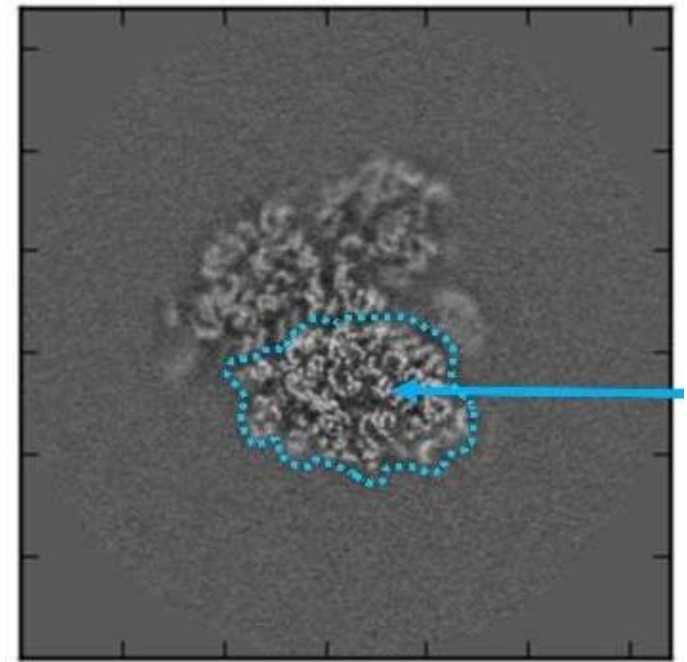


refinement of the individual
60S and 40S ribosomal subunits



refinement of the individual
60S subunit, 40S body and 40S head regions

2.5 2.8 3.1 3.4 3.8 4.1 4.6 5.0 [Å]



Natchiar *et al.*, *Nature* 2017.

See also: von Loeffelholz *et al.*, *Curr. Opin. Struct. Biol.* 2017.

Specific tips on focused refinement:

- works best after 3D classification / sorting
 - makes sure that it corresponds to a conformational / functional state, therefore the PDB requires to deposit the low-resolution map before focused refinement
 - provides a composite map
- further improves with partial signal subtraction (Bai *et al.*, 2015)
- localized reconstruction of subunits on viruses (Ilca *et al.*, 2015)
- subunit subtraction and focused refinement on GroEL (Roh *et al.*, 2017)
- re-centering focused region helps (alignment quality); e.g. Blees *et al.*, 2017
- dynamic signal subtraction (Schoebel *et al.*, 2017)
- multi-body refinement (Nakane *et al.*, 2018)

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